

**MTS Lecture -- American Rock Mechanics Association**

49th U.S. Rock Mechanics / Geomechanics Symposium

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***Thermo-Poro-Mechanics of Strain Localization  
in Rapidly Sheared Granular Rock, and  
Implications for Earthquake Source Physics***

**James R. Rice (Harvard)**

***Underlying studies done collaboratively with some of:***

**Nicolas Brantut (Univ Col Lond)**    **Massimo Cocco (INGV Rome)**

**Eric Dunham (Stanford Univ)**    **Nadia Lapusta (Caltech)**

**Hiroyuki Noda (JAMSTEC)**    **John Platt (Carnegie Inst Wash)**

**Alan Rempel (Univ Oregon)**    **John Rudnicki (Northwestern)**

## *Quandary in seismology:*

- Lab (J. Byerlee et al.) and field (M. D. Zoback et al.) estimates of friction coefficient are usually high,  $f \sim 0.6-0.8$ .

Shear strength  $\tau = f \times (\sigma_n - p)$ , where:

$\sigma_n$  = normal stress clamping the fault shut

$p$  = pore pressure in infiltrating fluid phase

- Fault slip zones are thin (despite wide damage zones of  $1-10^3$  m).

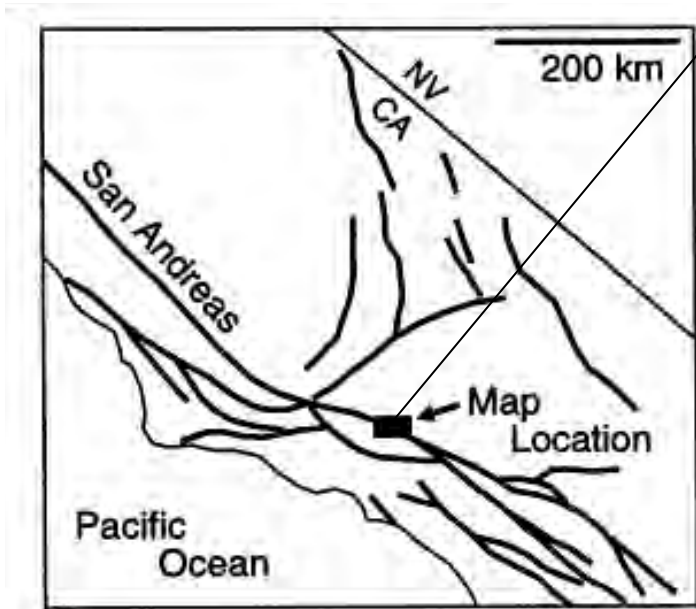
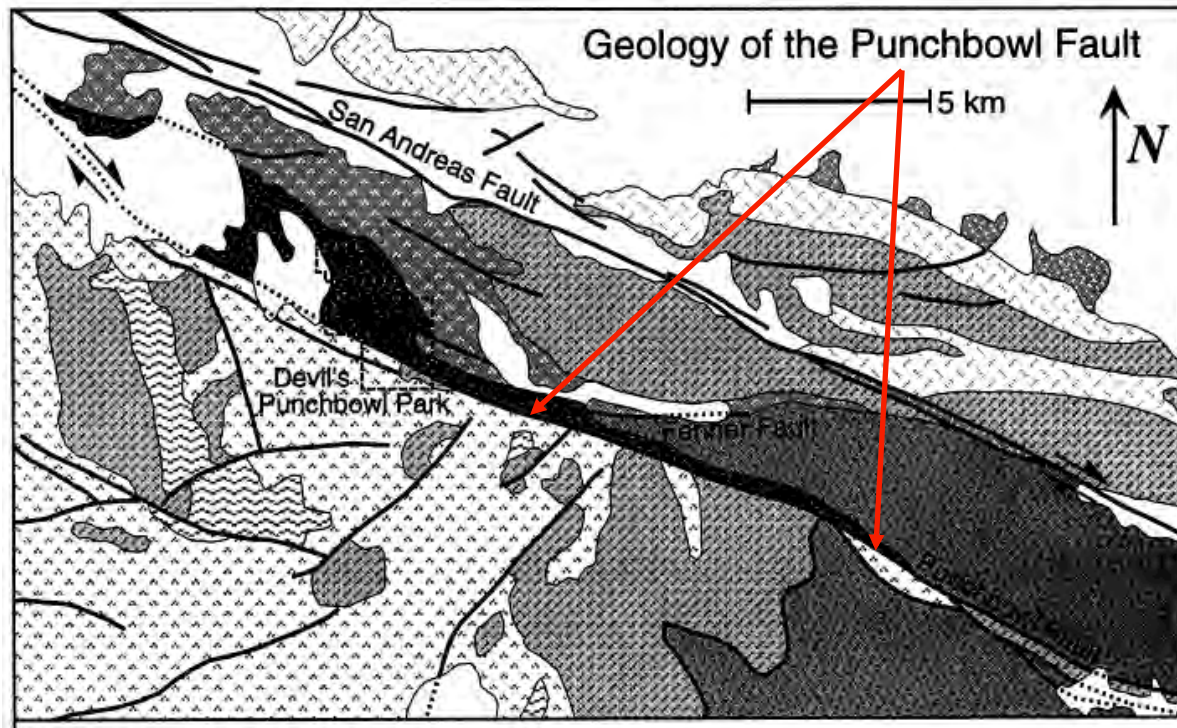
==> If those  $f$  prevail during seismic slip, and  $p \sim$  hydrostatic, we should find

- *measurable heat outflow* near major faults, and/or
- *extensive melt* signatures along exhumed faults.

Neither effect is generally found.

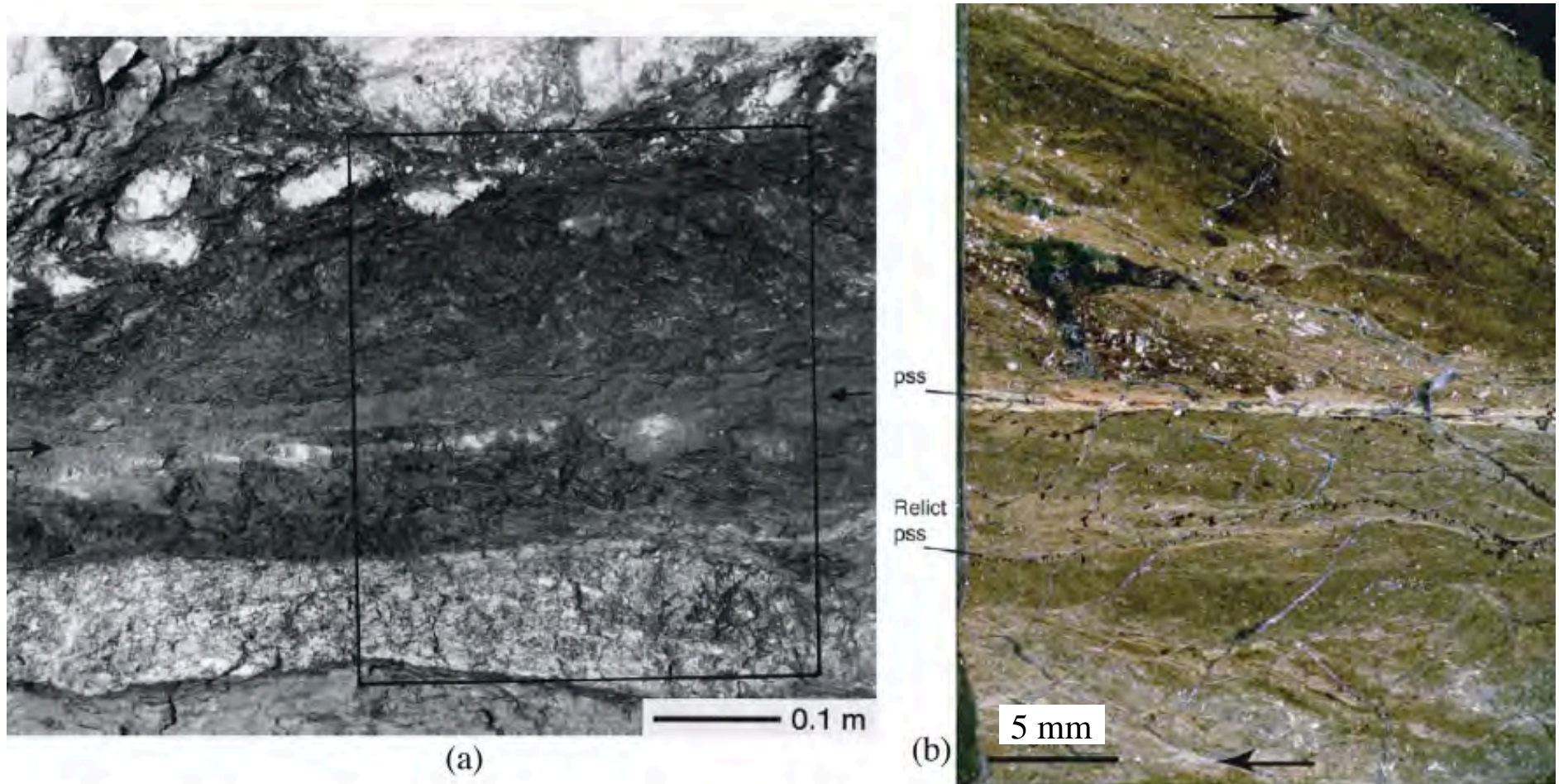
Chester &  
Chester

[*Tectonophys.*,  
1998]



# Earthquake shear is highly localized!

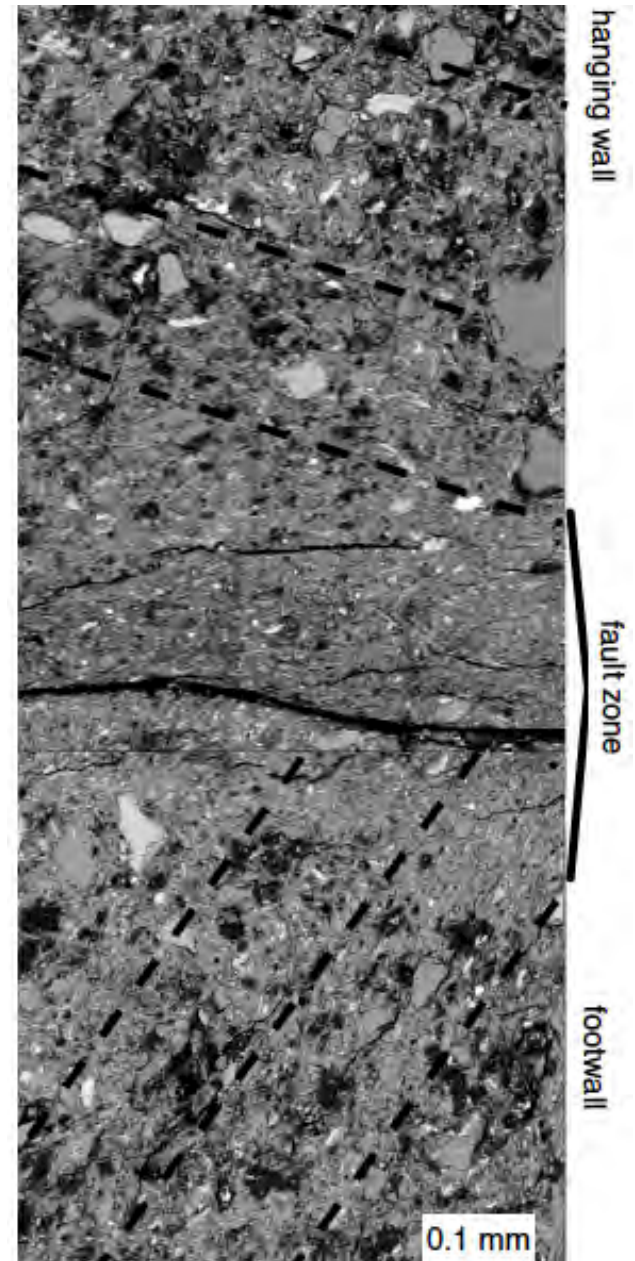
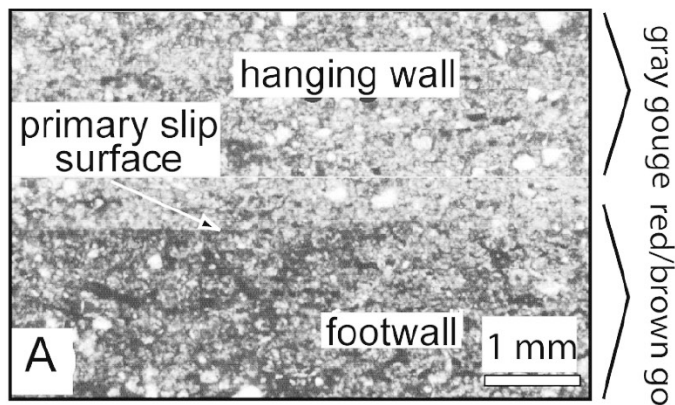
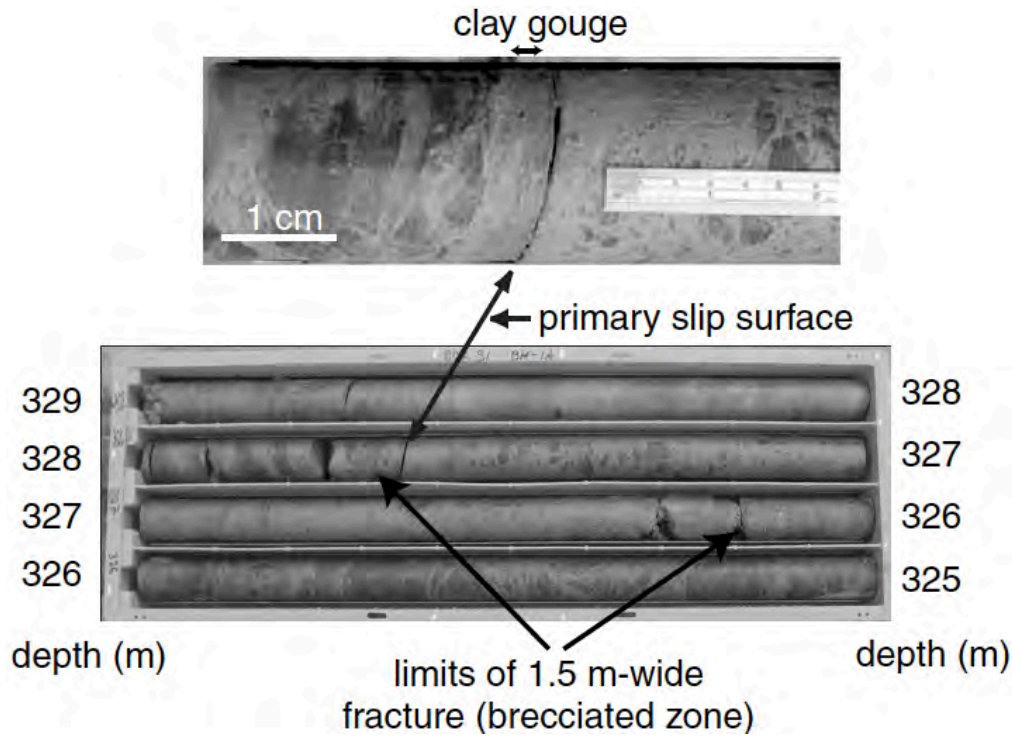
Punchbowl PSS, composite based on Chester & Chester [*Tectonophysics* '98] & Chester & Goldsby [*SCEC* '03]



**Figure 1.** Principal slip surface (PSS) along the Punchbowl fault. (a) From *Chester and Chester* [1998]: Ultracataclasite zone with PSS marked by black arrows; note 100 mm scale bar. (b) From Chester et al. (manuscript in preparation, 2005) [also *Chester et al.*, 2003; *Chester and Goldsby*, 2003]: Thin section; note 5 mm scale bar and  $\sim 1$  mm localization zone (bright strip when viewed in crossed polarizers due to preferred orientation), with microshear localization of most intense straining to  $\sim 100$ – $300$   $\mu\text{m}$  thickness.

[Heermance, Shipton & Evans, *BSSA*, 2003]

**Core retrieved across the Chelungpu fault, which hosted the 1999 Mw 7.6 Chi-Chi, Taiwan, earthquake: Suggests slip at 328 m depth traverse was accommodated within a zone ~ 50–300  $\mu\text{m}$  thick.**

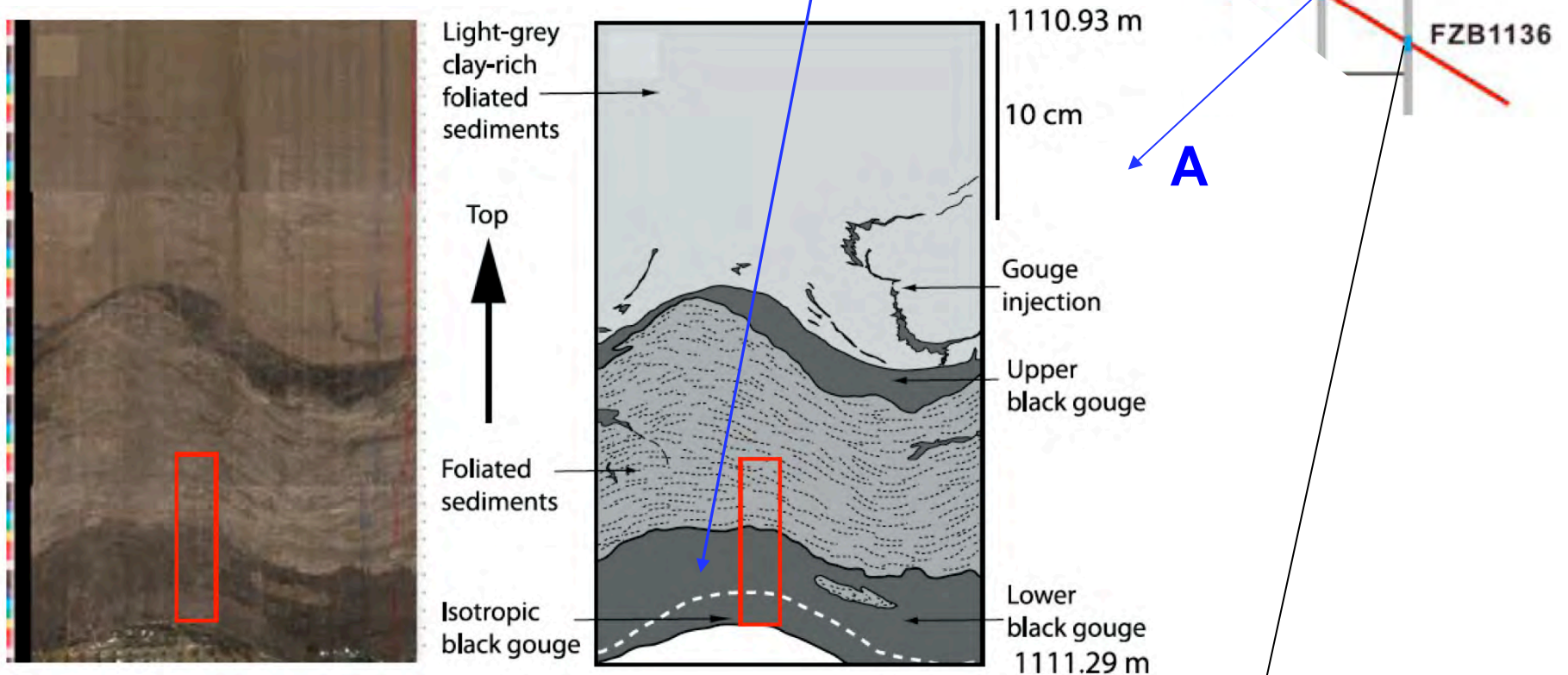


## Two other Chelungpu Fault, Taiwan boreholes

[Boullier et al., GGG 2009, GSL 2011]:

### Principal Slip Zone (PSZ) localized within black gouges

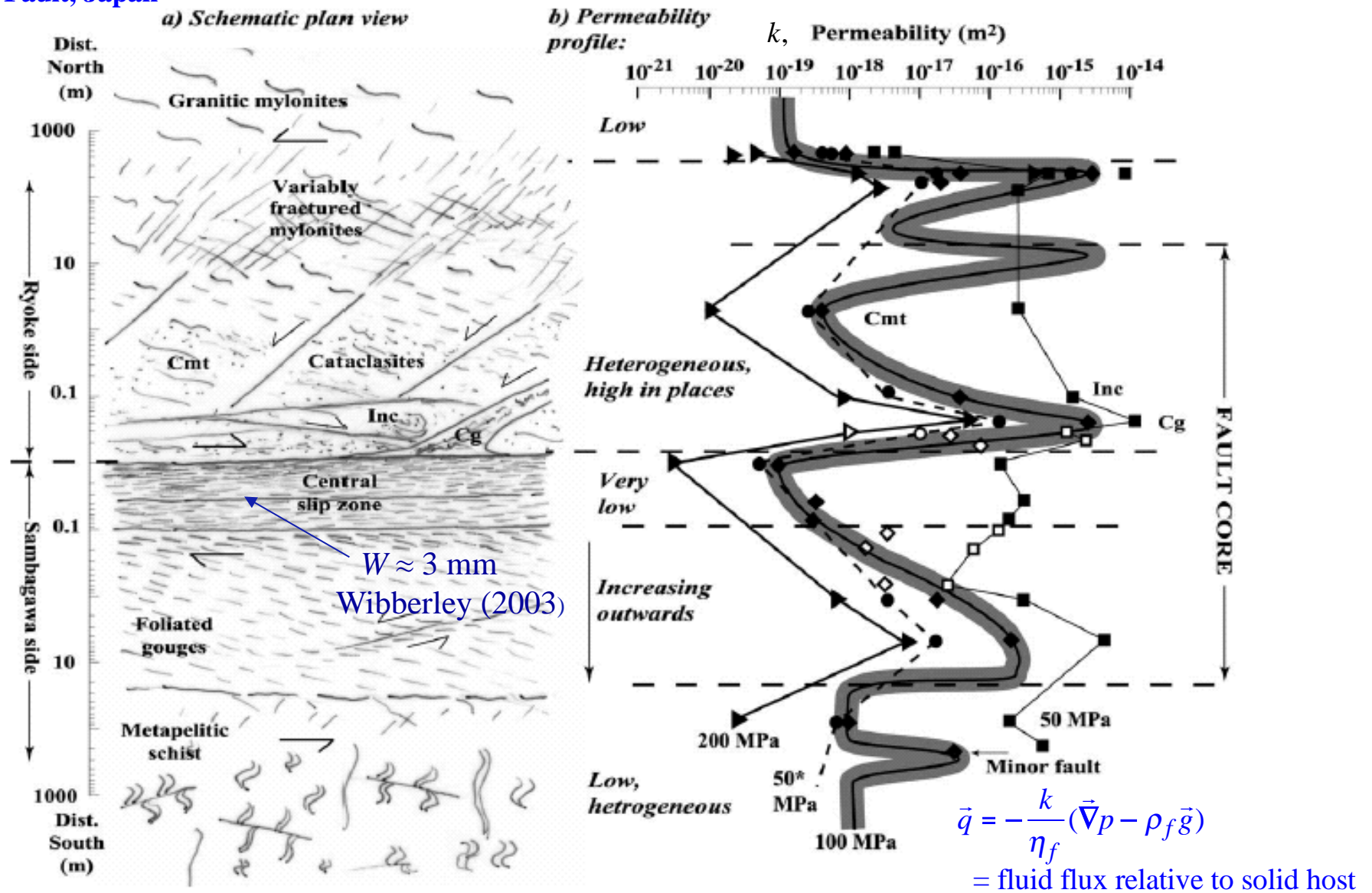
- Hole A, fault at 1111 m depth: PSZ is ~2 cm thick



Unrolled scanning image of FZA1111 and corresponding sketch

- Hole B, fault at 1136 m depth: PSZ is ~3 mm thick

PSZ layering defined by variations in concentrations of clay minerals and clasts, comparable to structures produced in high-rate rotary shear exp's.



**This study:** Primary source of data we use for gouge **porosity**, **compressibility** and **permeability** as functions of effective confining stress (and its history).

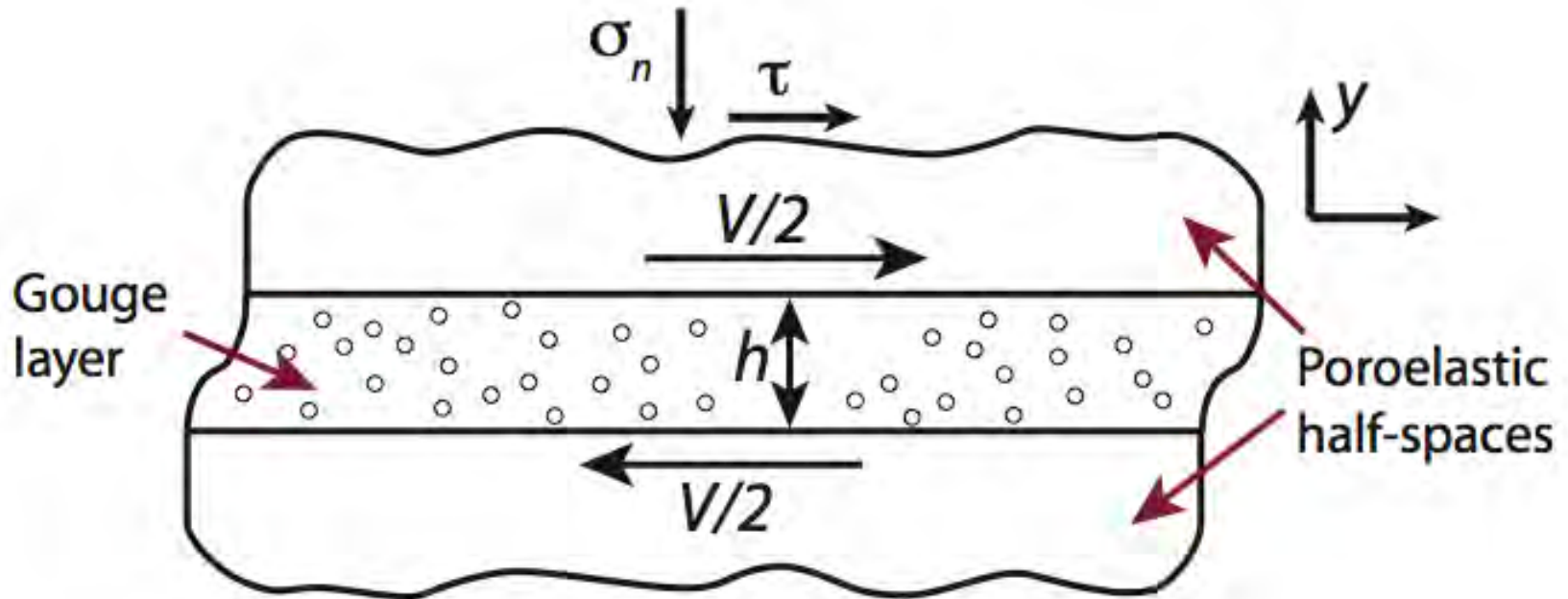
$$\tau = f \times (\sigma_n - p)$$

*Statically strong but dynamically weak faults, e.g., due to thermal weakening in rapid, large slip:*

- *Process expected to be important from start of seismic slip:*
  - Thermal pressurization of in-situ pore fluid,  
reduces effective stress.
- *Process that may set in at large enough rise in T:*
  - Thermal decomposition, fluid product phase at high pressure  
(e.g., CO<sub>2</sub> from carbonates; H<sub>2</sub>O from clays or serpentines).
- *Ultimately:*
  - Melting at large slip, *if* above have not limited increase of T.



## Shear of a fluid-saturated gouge layer



- Two non-yielding half-spaces are moved relative to each other at a speed  $V$  (typically,  $V \sim 1$  m/s).
- All inelastic deformation accommodated in gouge layer, leading to a nominal strain rate  $\dot{\gamma}_0 = V / h$ .

## Thermo-mechanical model in gouge layer

- To model the deforming gouge layer we use,

Mechanical equilibrium  $\frac{\partial \tau}{\partial y} = 0, \quad \frac{\partial \sigma_n}{\partial y} = 0$

Conservation of energy  $\frac{\partial T}{\partial t} - \alpha_{th} \frac{\partial^2 T}{\partial y^2} = \frac{\tau \dot{\gamma}}{\rho c}$

Conservation of fluid mass  $\frac{\partial p}{\partial t} - \alpha_{hy} \frac{\partial^2 p}{\partial y^2} = \Lambda \frac{\partial T}{\partial t}$

- Shear stress modeled using the effective stress and **rate-strengthening** friction,

$$\tau = f(\dot{\gamma})(\sigma_n - p) \quad f(\dot{\gamma}) = f_0 + (a - b) \log\left(\frac{\dot{\gamma}}{\dot{\gamma}_0}\right)$$

(We assume  $a - b \equiv \left(\dot{\gamma} \frac{df(\dot{\gamma})}{d\dot{\gamma}}\right)_{\dot{\gamma}=\dot{\gamma}_0} > 0$ )

**Shear between moving rigid blocks of perfectly insulating, impermeable material :**

**Exact homogeneous shear solution (Lachenbruch, JGR, 1980, version ignoring dilatancy) :**

$$\tau(t) = f_o (\sigma_n - p(t)) = f_o (\sigma_n - p_a) \exp\left(-f_o \frac{\Lambda V t}{\rho c h}\right),$$

*(Exponential decay of strength with slip)*

**Linearized perturbation analysis :**

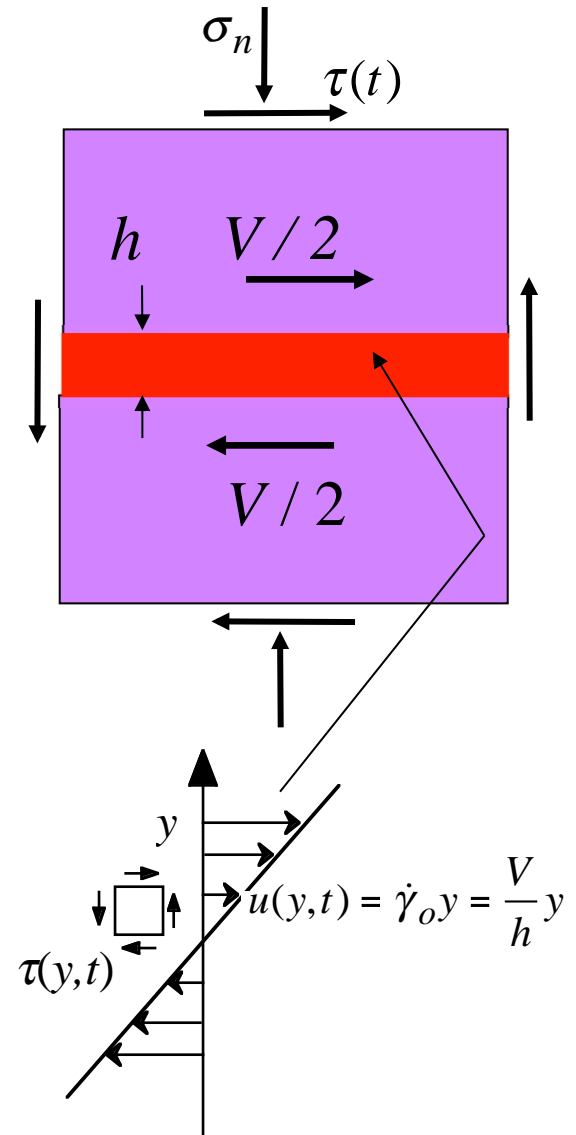
**Is that solution stable to small perturbations?**

*Not unless h is very small !*

Stable only if  $h \leq W_{crit} \equiv \frac{\pi^2}{\left(2 + \frac{f_o}{a-b}\right)} \frac{\rho c}{f_o \Lambda} \frac{(\alpha_{th} + \alpha_{hy})}{V}$ .

$\left( \text{Typically, } \frac{f_o}{a-b} \gg 2 \Rightarrow W_{crit} \approx \pi^2 \frac{a-b}{f_o^2} \frac{\rho c}{\Lambda} \frac{\alpha_{th} + \alpha_{hy}}{V} \right)$

[ $W_{crit} = \lambda_{shr} / 2$ , where  $\lambda_{shr}$  = longest wavelenth  $\lambda$  for stable linearized response to infinitesimal  $\exp(2\pi iy / \lambda)$  perturbation]



Rice, Rudnicki & Platt (JGR 2014)

*Estimates of maximum stable shear layer thickness (i.e., localized zone width)  $W_{crit}$*

Results, using  $f_o = 0.4$ ,  $\frac{f_o}{a-b} = 20$ ,  $V = 1 \frac{\text{m}}{\text{s}}$ ,  $\alpha_{th} = 0.7 \frac{\text{mm}^2}{\text{s}}$ ,  $\rho c = 2.7 \frac{\text{MPa}}{\text{°C}}$  :

**Corresponding to ~ 7 km depth :**

*Low estimate* (Based on lab properties of *intact* Median Tectonic Line gouge [Wibberley and Shimamoto, 2003] at effective confining stress = 125 MPa and  $T = 200\text{°C}$ ):

$$\Lambda = 0.70 \frac{\text{MPa}}{\text{°C}}, \quad \text{and} \quad \alpha_{hy} = 1.5 \frac{\text{mm}^2}{\text{s}} \quad \Rightarrow \quad W_{crit} = 3-5 \mu\text{m}$$

*High estimate* (Accounts very roughly for *fresh damage* of the initially intact fault gouge, introduced at the rupture front just before and during shear, by increasing permeability  $k$  to  $k^{dmg} = 5-10 k$ , and increasing drained compressibility  $\beta_d$  to  $\beta_d^{dmg} = 1.5-2 \beta_d$ ):

$$\Lambda \approx 0.34 \frac{\text{MPa}}{\text{°C}}, \quad \text{and} \quad \alpha_{hy} \approx 3.5 \frac{\text{mm}^2}{\text{s}} \quad \Rightarrow \quad W_{crit} \approx 25-40 \mu\text{m}$$

**Corresponding to ~ 1 km depth :**

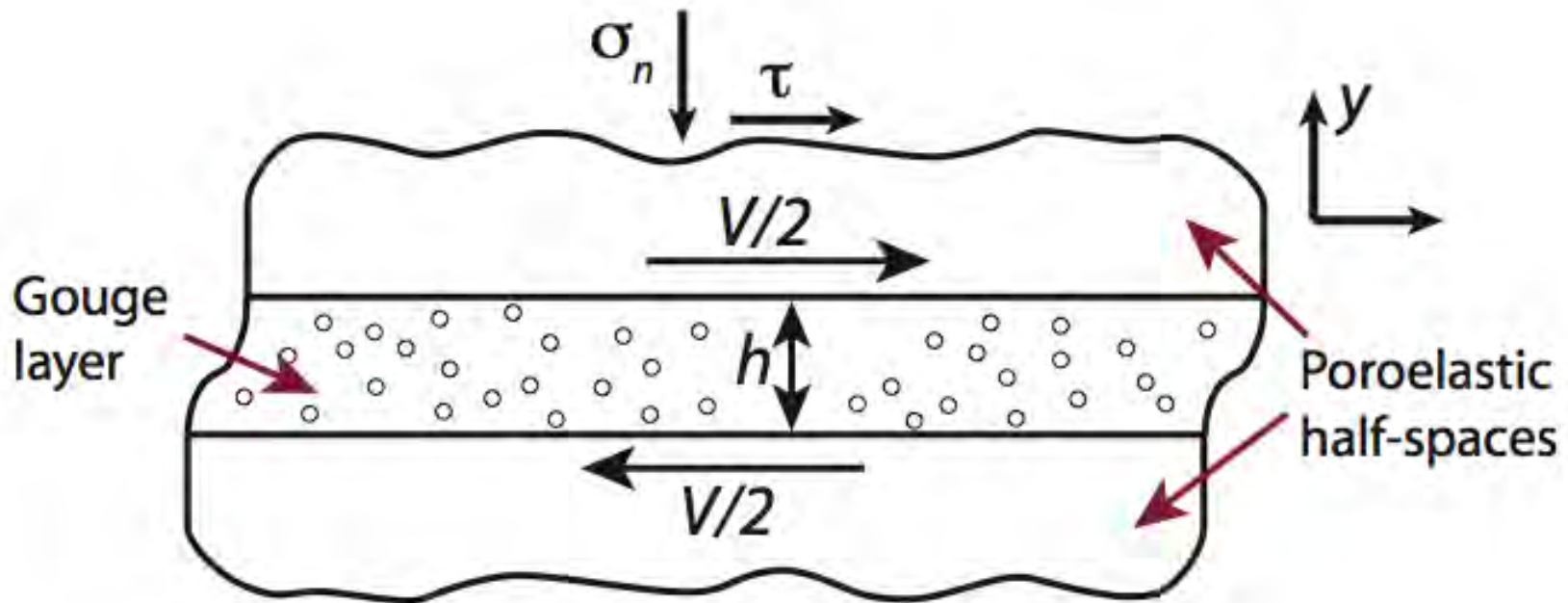
*Low estimate* :  $W_{crit} \sim 25 \mu\text{m}$

*High estimate* :  $W_{crit} \sim 200 \mu\text{m}$

## ***Now: Full nonlinear numerical solution results***

[Platt, Rudnicki, and Rice, JGR 2014]

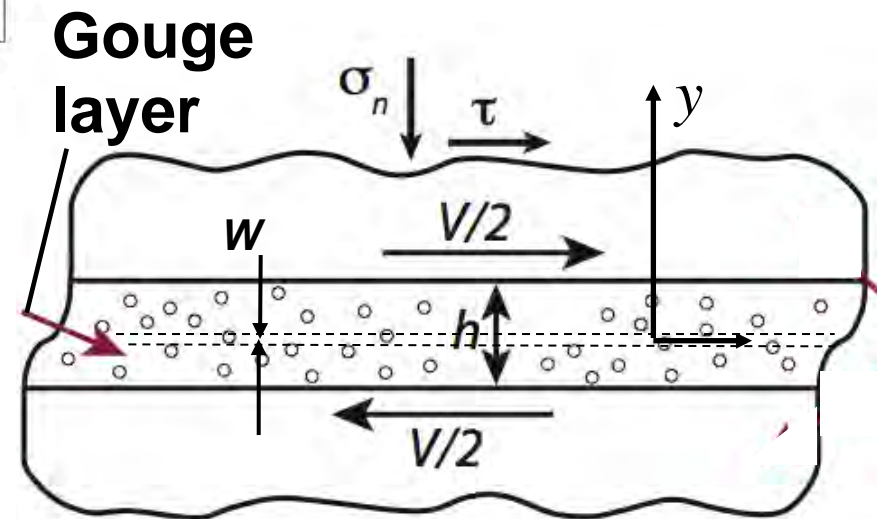
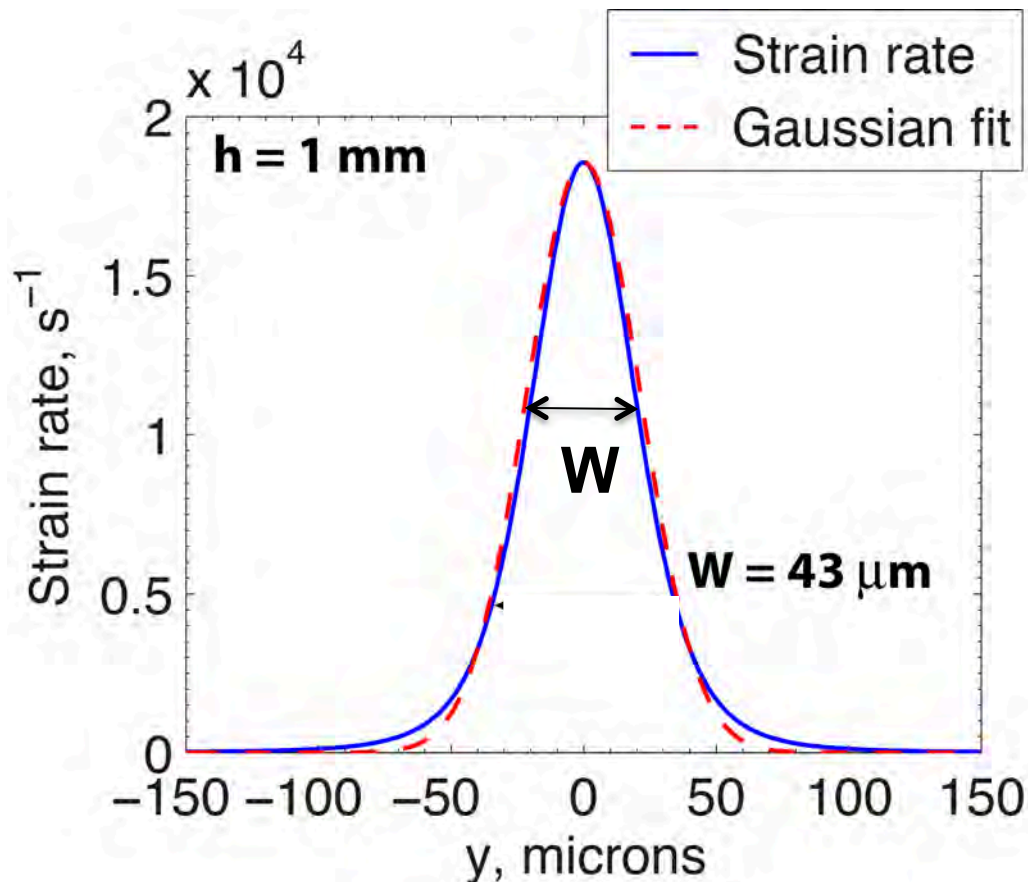
### Shear of a fluid-saturated gouge layer



- Two non-yielding half-spaces are moved relative to each other at a speed  $V$  (typically,  $V \sim 1$  m/s).
- All inelastic deformation accommodated in gouge layer, leading to a nominal strain rate  $\dot{\gamma}_0 = V / h$ .

## Strain localization

- Full nonlinear numerical simulations (vs. linear perturbations), using representative physical values predict that strain localization does occur.

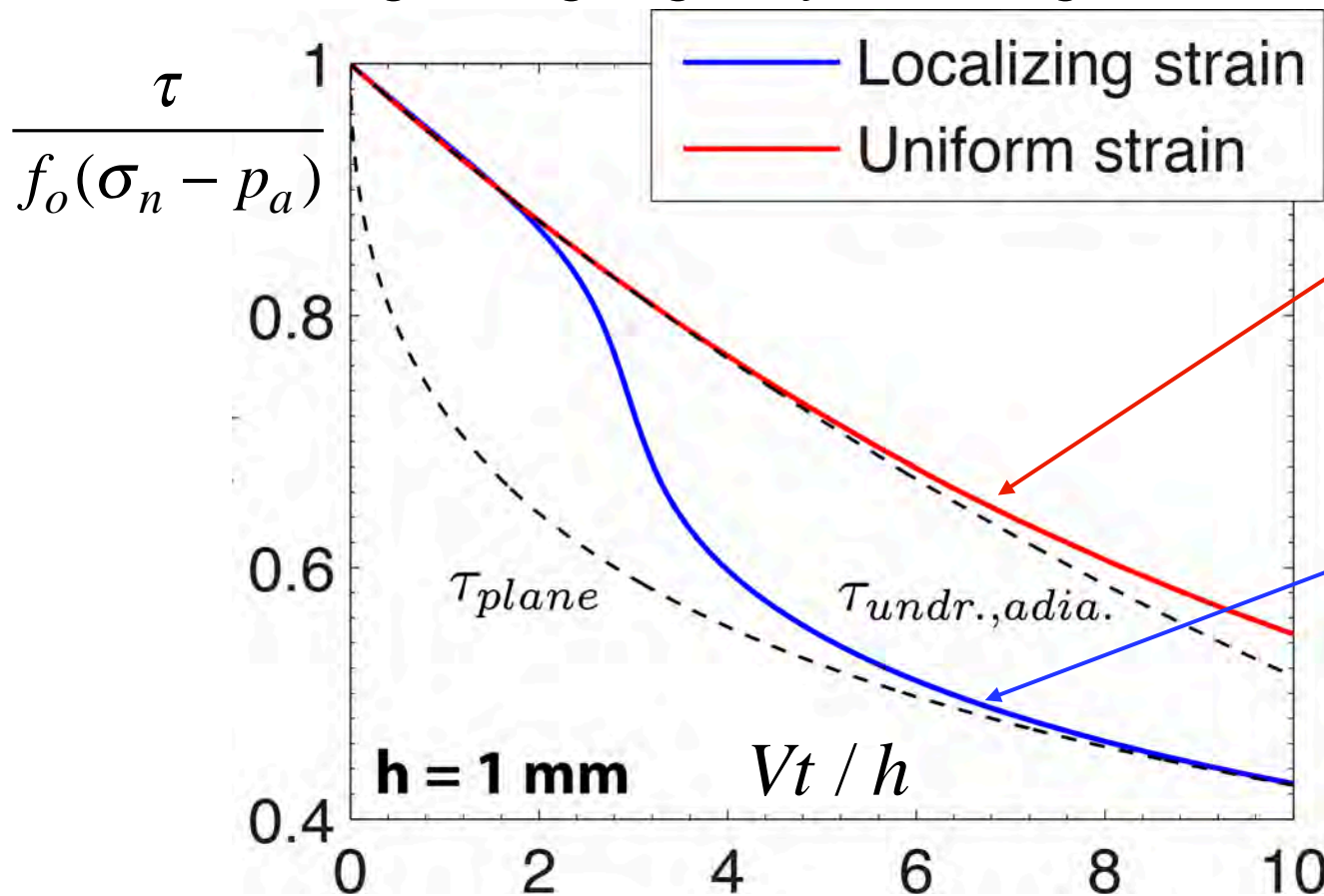


- Deformation has localized to a zone much thinner than the layer,  $W \ll h$  ( $43 \mu m \ll 1,000 \mu m$ ).

$W_{\text{nonlin. calc.}}$  is comparable to  $W_{\text{lin. pert.}}$  .

# Implications, dynamic weakening

- Weakening of a gouge layer during localization



Closely follows Lachenbruch [JGR, 1980] sol'n (Here, transport at boundary allowed).

Closely follows "slip on a plane" Rice [JGR, 2006] sol'n, generalizing Mase & Smith [JGR, 1987] sol'n.

- Localization leads to additional weakening.

$$\tau = f_o(\sigma_n - p_a) \exp\left(\frac{Vt}{L^*}\right) \operatorname{erfc}\left(\sqrt{\frac{Vt}{L^*}}\right) \quad \text{where } L^* = \left(\frac{2\rho c}{f_o\Lambda}\right)^2 \frac{\left(\sqrt{\alpha_{hy}} + \sqrt{\alpha_{th}}\right)^2}{V}$$

$$\tau = f \times (\sigma_n - p)$$

Statically strong but dynamically weak faults, e.g., due to thermal weakening in rapid, large slip:

- *Process expected to be important from start of seismic slip:*
  - Thermal pressurization of in-situ pore fluid,  
reduces effective stress.
- *Process that may set in at large enough rise in T:*
  - Thermal decomposition, fluid product phase at high pressure  
(e.g., CO<sub>2</sub> from carbonates; H<sub>2</sub>O from clays or serpentines).
- *Ultimately:*
  - Melting at large slip, *if* above have not limited increase of T.



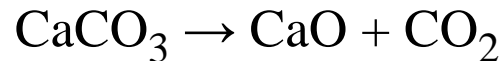
***Examples, thermal decomposition:***

***Dolomite, CaMg(CO<sub>3</sub>)<sub>2</sub>*** (De Paola et al., *Tectonics*, 2008, *Geology*, 2011; Goren et al., *J. Geophys. Res.*, 2010):

- At  $T \sim 550^\circ\text{C}$ , dolomite decomposes to calcite, periclase, and carbon dioxide:



- At  $T \sim 700\text{-}900^\circ\text{C}$ , the calcite further decomposes to lime and carbon dioxide:



***Many clays and hydrous silicates*** (Brantut et al., *J. Geophys. Res.*, 2010):

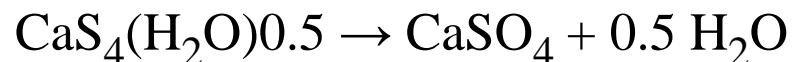
- At  $T \sim 500^\circ\text{C}$  ( $\sim 300^\circ\text{C}$  for smectite,  $\sim 800^\circ\text{C}$  for chlorite), decomposition releasing  $\text{H}_2\text{O}$  starts.

***Gypsum, CaSO<sub>4</sub>(H<sub>2</sub>O)<sub>2</sub>*** (Brantut et al., *Geology*, 2010):

- At  $T \sim 100^\circ\text{C}$ , gypsum dehydrates to form bassanite:

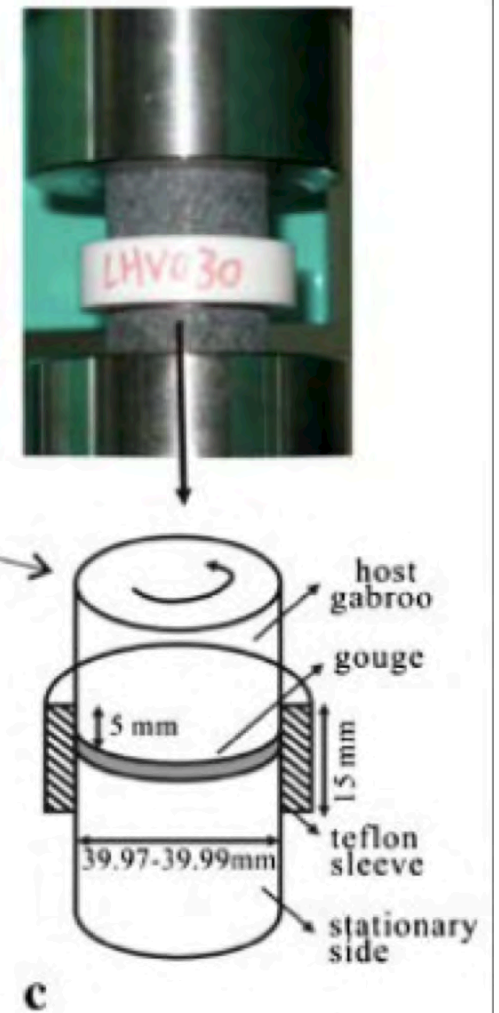
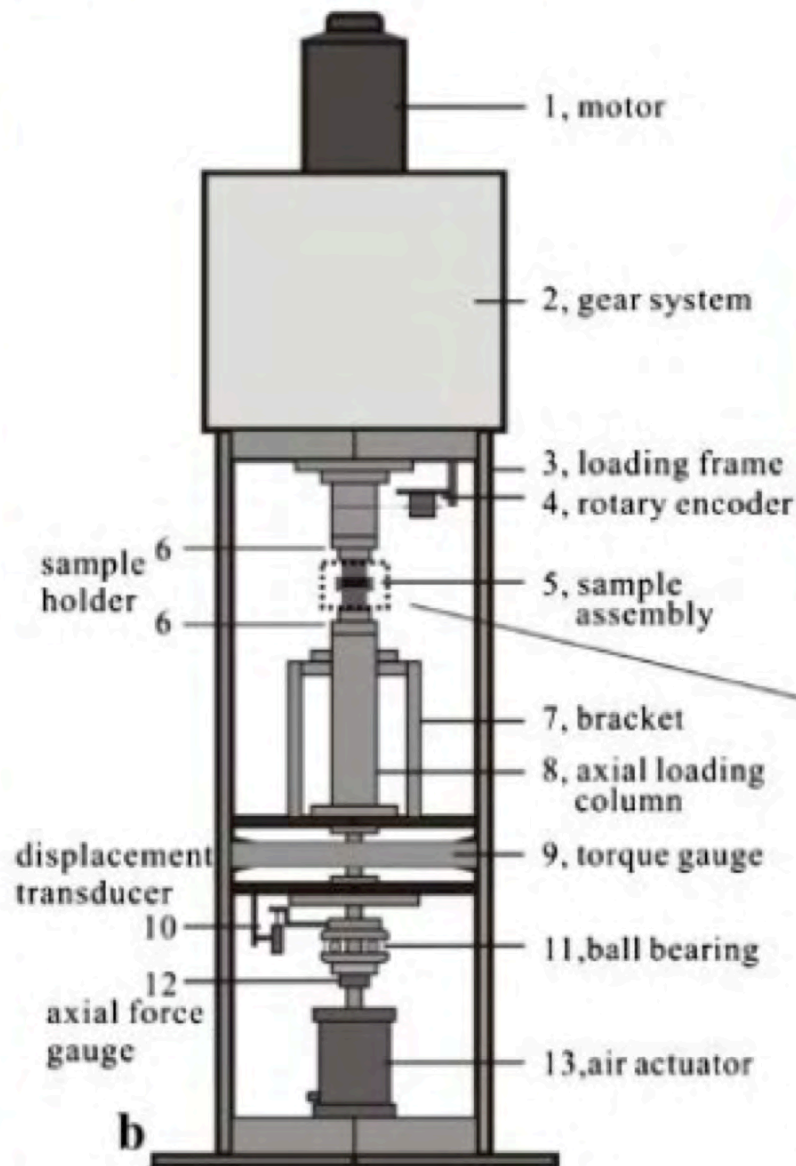


- At  $T \sim 140^\circ\text{C}$ , bassanite turns into anhydrite



# Example, recent version of Toshi Shimamoto's rotary shear apparatus (at Institute of Geology, Peking University)

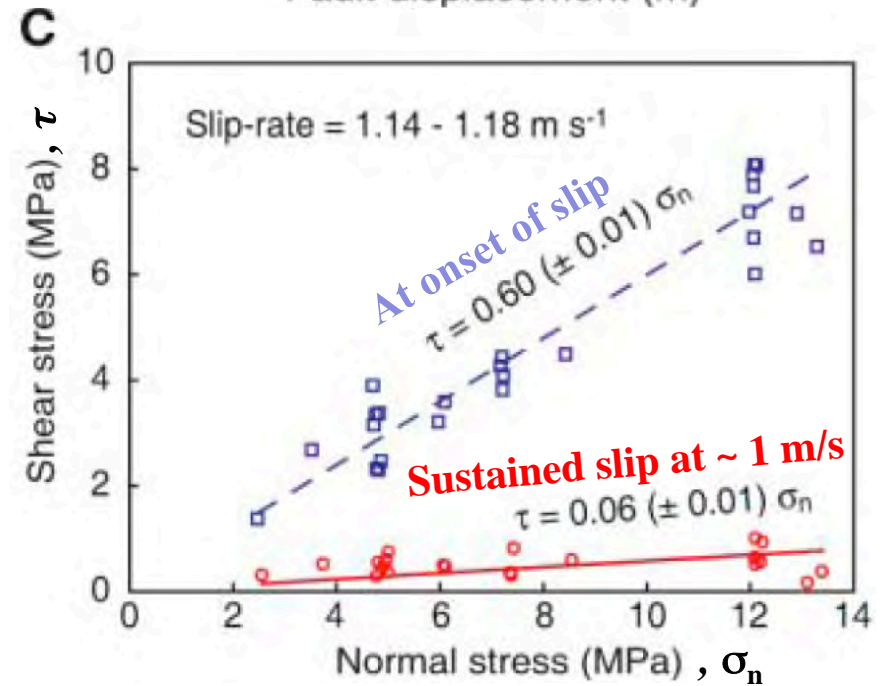
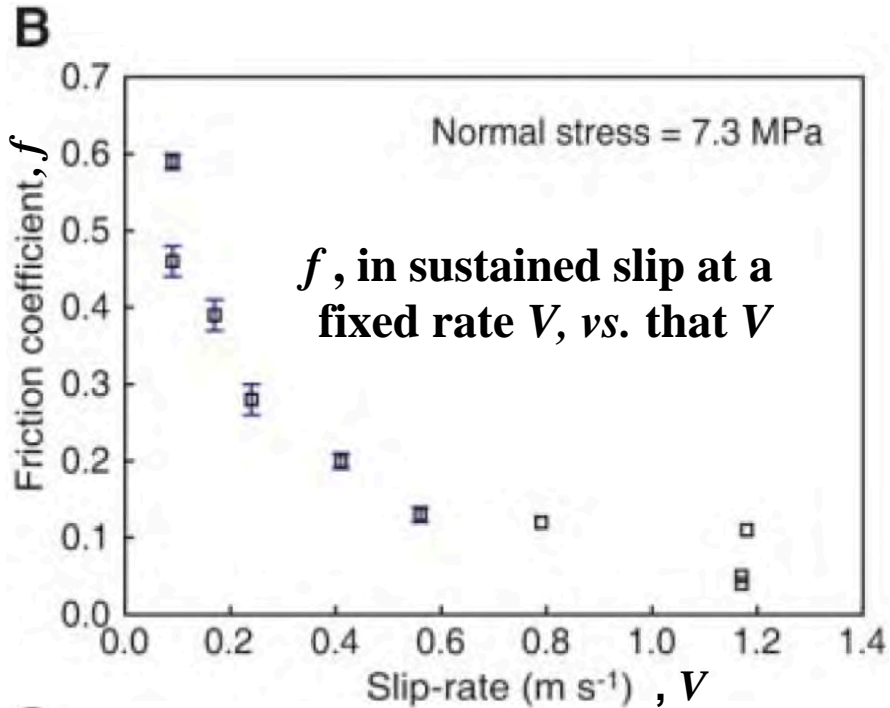
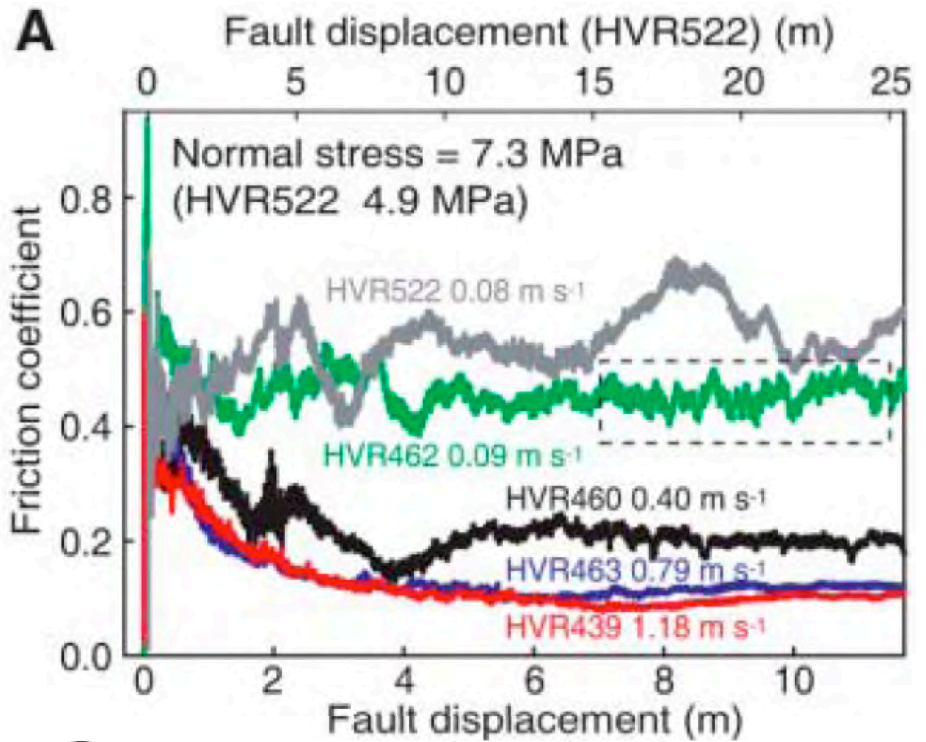
*J. Chen et al. / Tectonophysics xxx (2013) xxx-xxx*



[Han, Shimamoto, Hirose, Ree & Ando, *Sci.*, 2007]:

### Carbonate Faults

Simulated faults in Carrara Marble at subseismic to seismic slip rates

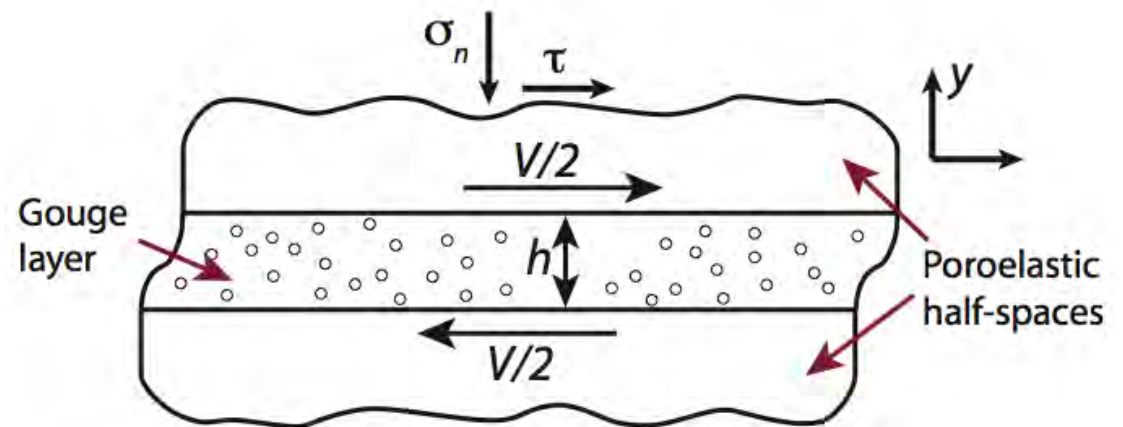


# Model for decomposing gouge material

- To model the deforming gouge layer we use, based on J. Sulem, I. Vardoulakis, and co-workers (Brantut, Ghabezloo, Famin, Lazar, Noda, Schubnel, Stefanou, Veveakis, ...),

$$\frac{\partial T}{\partial t} = \frac{\tau \dot{\gamma}}{\rho c} + \alpha_{th} \frac{\partial^2 T}{\partial y^2} - E_r \frac{\partial \xi}{\partial t}$$

$$\frac{\partial p}{\partial t} = \Lambda \frac{\partial T}{\partial t} + \alpha_{hy} \frac{\partial^2 p}{\partial y^2} + P_r \frac{\partial \xi}{\partial t}$$



- We assume that the reaction follows an Arrhenius kinetic law,

$$\frac{\partial \xi}{\partial t} = A (1 - \xi) \exp\left(-\frac{Q}{RT}\right)$$

Platt, Brantut & Rice (*JGR*, 2015)

Table 2. List of reaction parameters.

Parameter	Platt, Brantut & Rice ( <i>JGR</i> , 2015)			
	Decarbonation reaction	Dehydration reactions		
	Calcite <sup>a</sup>	Lizardite <sup>b</sup>	Illite/muscovite <sup>c</sup>	Talc <sup>d</sup>
Pre-exponential factor, $\log_{10}(A)$ ( $A$ in 1/s)	15.47	17.80	6.92	14.30
Activation energy, $Q$ (kJ/mol)	319	328	152	372
Fluid mass, $m_{tot}^{100\%}$ (kg/m <sup>3</sup> ),	1140	240	150	131
Enthalpy <sup>e</sup> , $\Delta H$ (MJ/kg)	7.25	2.56	5.49	5.17
Solid volume change, $\phi$ ( $\times 10^{-3}$ m <sup>3</sup> /kg)	0.46	0.88	0.35	0.78
Fluid density, $\rho_f$ (m <sup>3</sup> /kg)	418	267	135	159
$T_r$	960 °C	885 °C	1733 °C	1454 °C
$E_r$ (°C)	$3.06 \times 10^3$	275	305	251
$P_r$ (GPa)	7.42	2.80	3.56	2.43
$W^{HT}$	5.1 $\mu\text{m}$	1.2 $\mu\text{m}$	1.1 $\mu\text{m}$	1.3 $\mu\text{m}$
$W$	12.7 $\mu\text{m}$	6.8 $\mu\text{m}$	11.9 $\mu\text{m}$	8.6 $\mu\text{m}$

***Linear perturbation results: very rough***

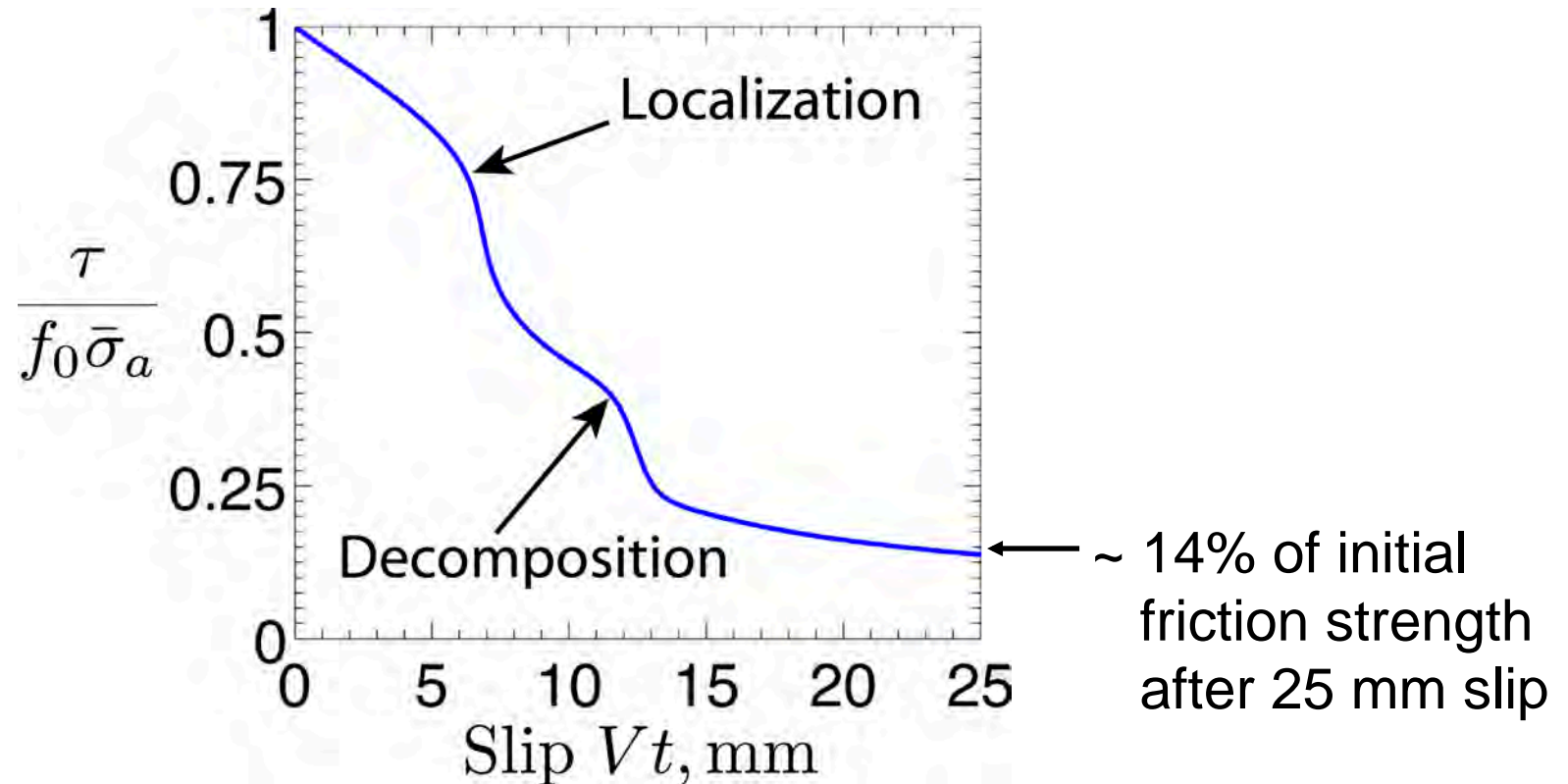
***estimates of localization zone widths :***

High  $T$ , fast reaction rate limit: 
$$W^{HT} \approx \pi^2 \frac{\alpha_{hy}}{V} \frac{(a-b)}{f_o^2} \frac{\rho c E_r}{P_r}$$

Low  $T$ , pre-reaction thermal press.: 
$$W \approx \pi^2 \frac{a-b}{f_o^2} \frac{\rho c}{\Lambda} \frac{\alpha_{th} + \alpha_{hy}}{V}$$

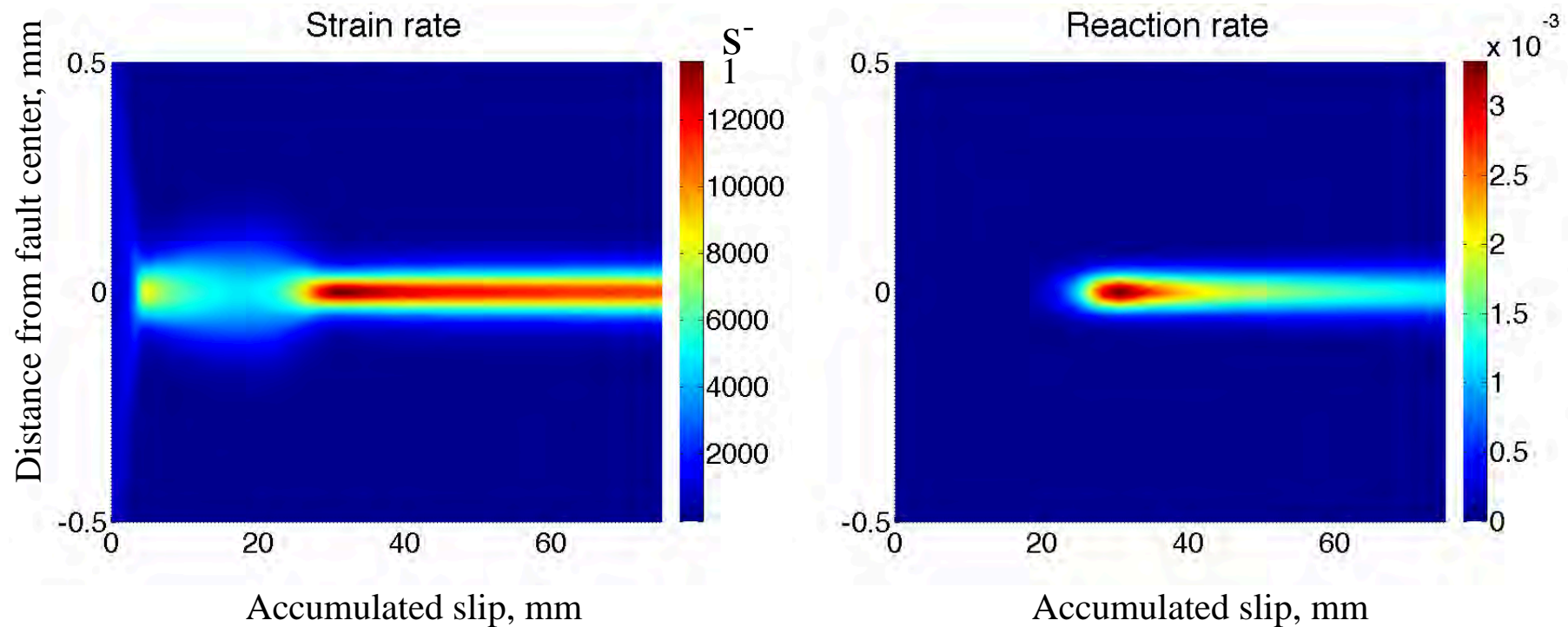
[ $W = \lambda / 2$ , where  $\lambda =$  longest wavelenth for stable linearized response to infinitesimal  $\exp(2\pi iy / \lambda)$  perturbation]

Representative simulations:  
thermal pressurization of in-situ fluids,  
followed by thermal decomposition



**Supports concept that faults may be *strong* but *brittle* (quickly lose strength after slip is initiated at a place of localized stress concentration)**

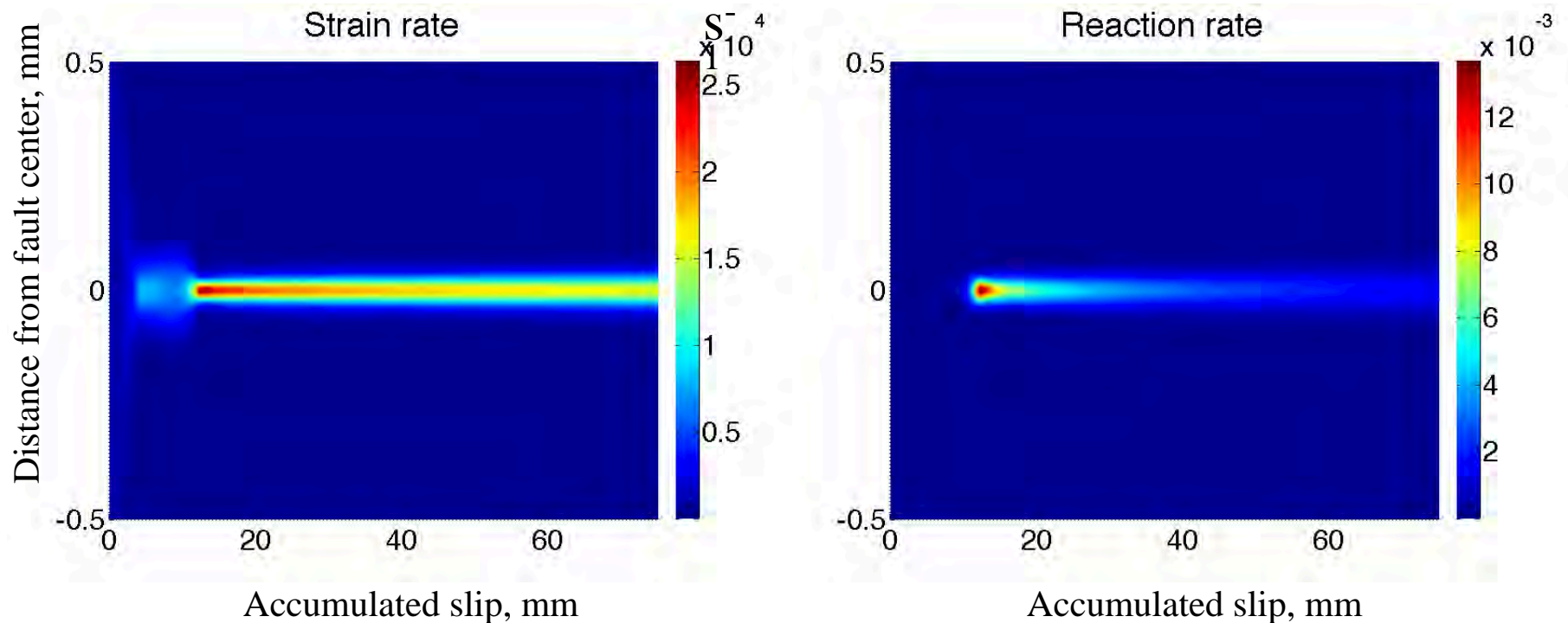
- Numerical solutions for a 1 mm wide gouge layer.



- When the reaction becomes important, we observe significant strain localization ( $W_{\text{nonlin. calc.}}$  of order  $\sim 2 \times W_{\text{lin. pert.}}$ ).

# Independence of reaction rate

- Our linear stability analysis predicts the localized zone width is independent of kinetic parameters. To test this we **increase  $A$  by three orders of magnitude.**



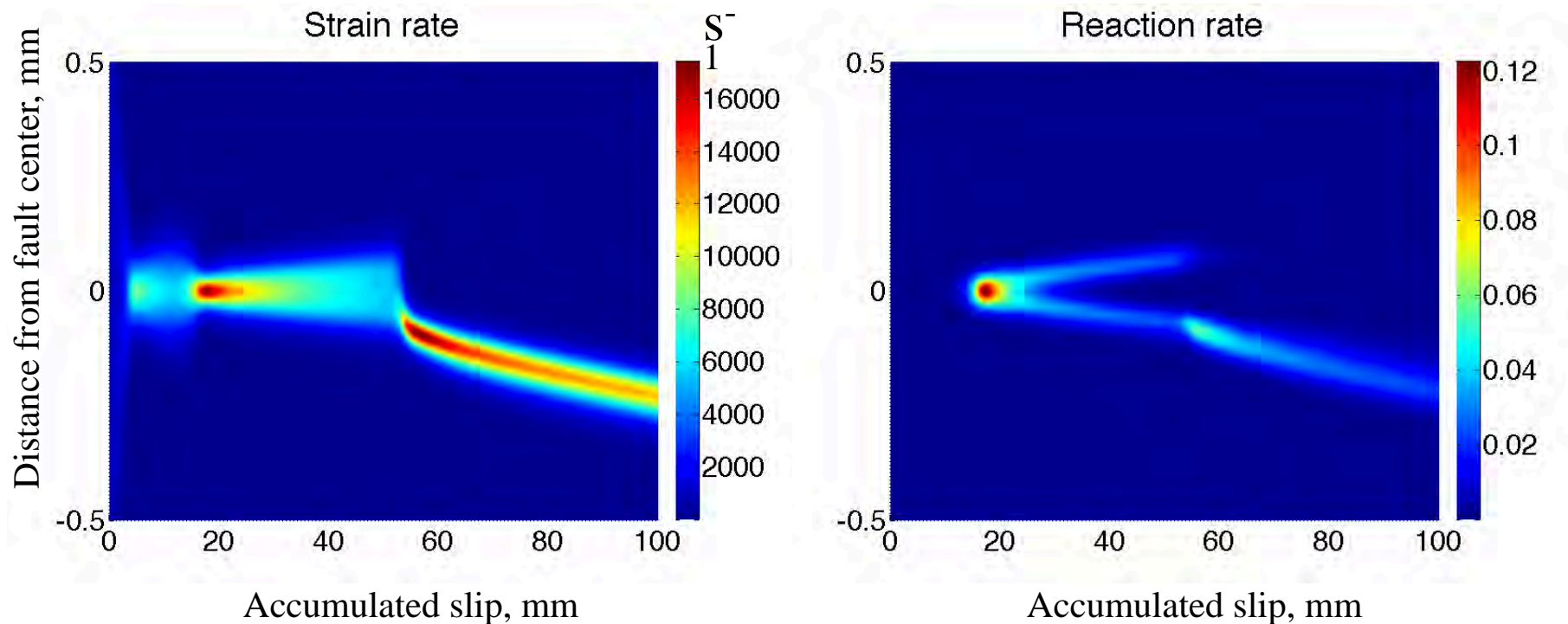
- The localized zone width has only decreased by a factor of two.

Platt, Brantut & Rice (AGU, Fall 2011; JGR 2015)



# Localized zone migration

- Now we investigate a case for which **depletion of reactant** is important.

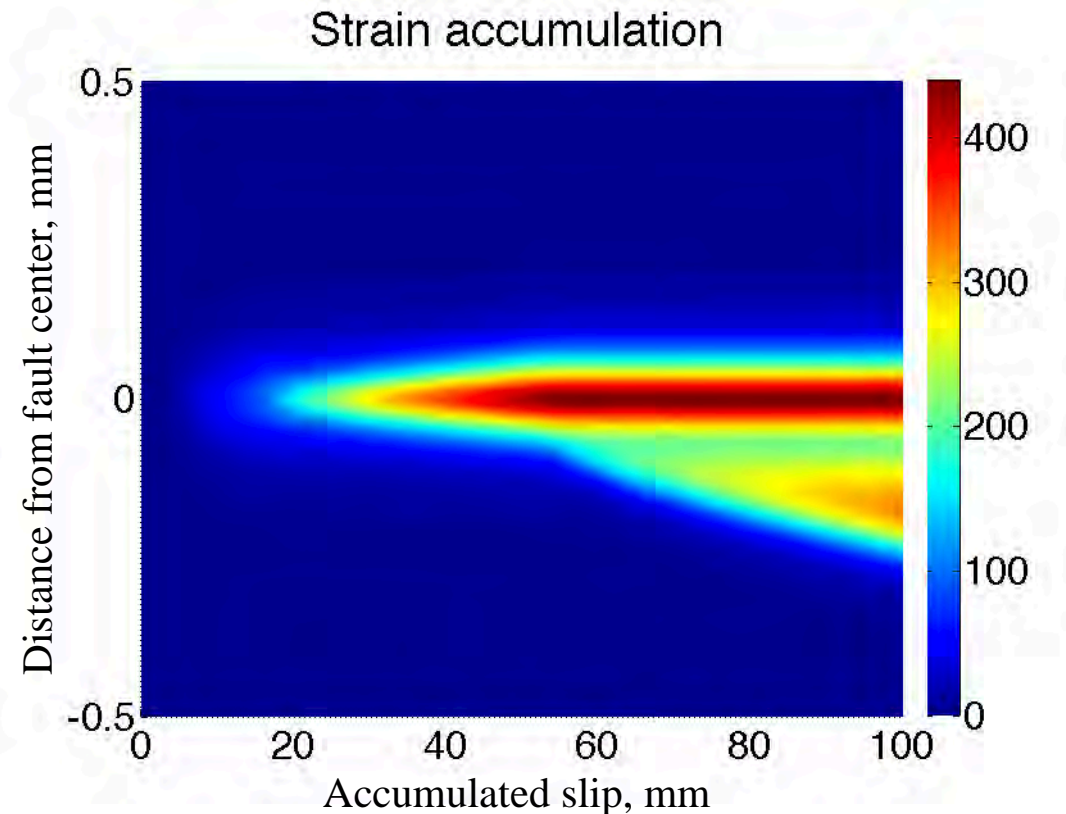


- Depletion causes the zone of localized straining to migrate. The strain rate and reaction rate profiles are strongly coupled.

Platt, Brantut & Rice (AGU, Fall 2011; JGR 2015)

# Localized zone migration

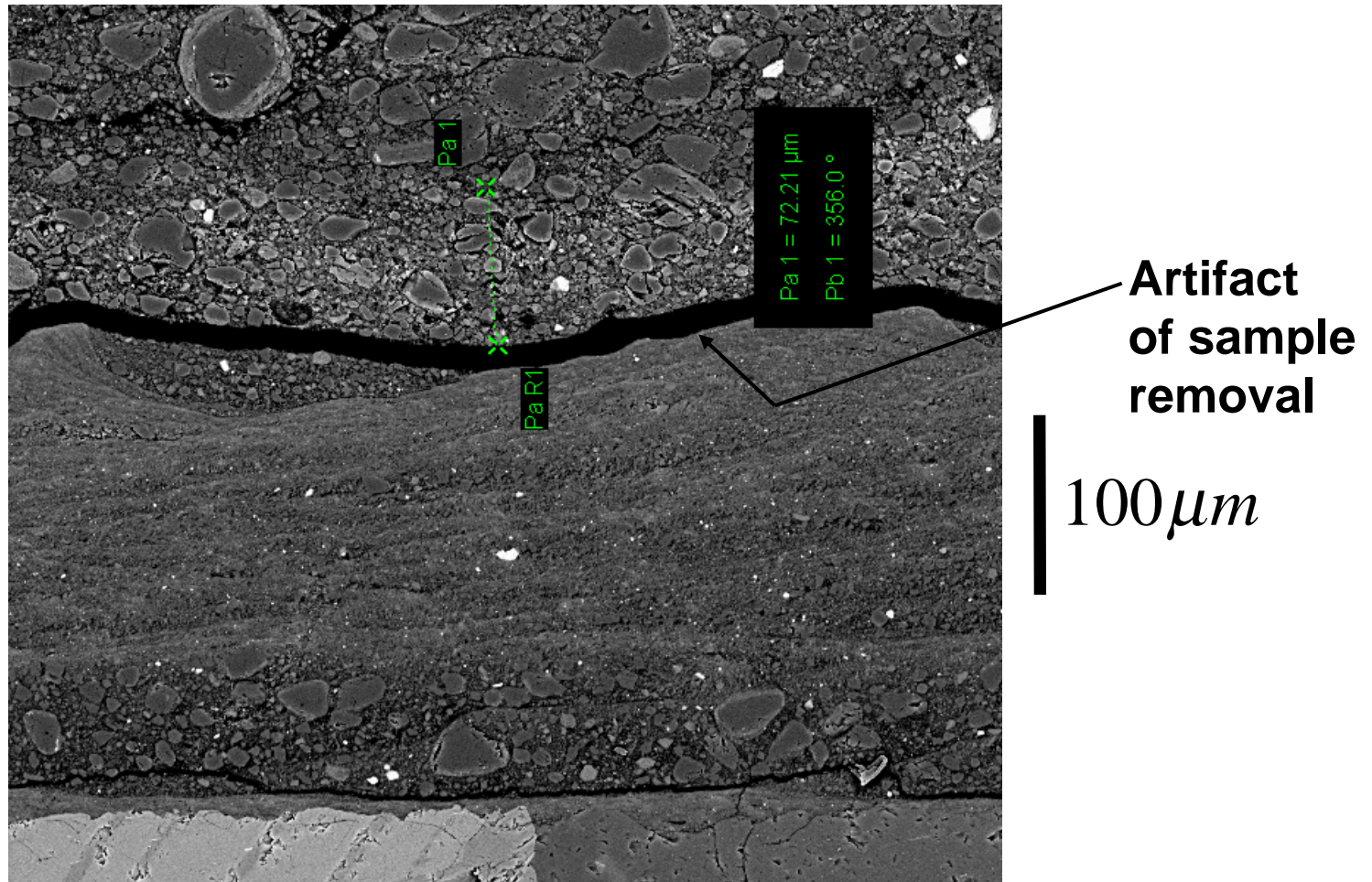
- This localized zone migration leads to a complex, non-monotonic, strain history.



- Possible end result: Laminations in gouge.

Platt, Brantut & Rice (*AGU*, Fall 2011; *JGR* 2015)

# Observation suggesting migration (in rotary shear of carbonate sample)



from T. Mitchell, Univ. Col. London (*private comm.*)

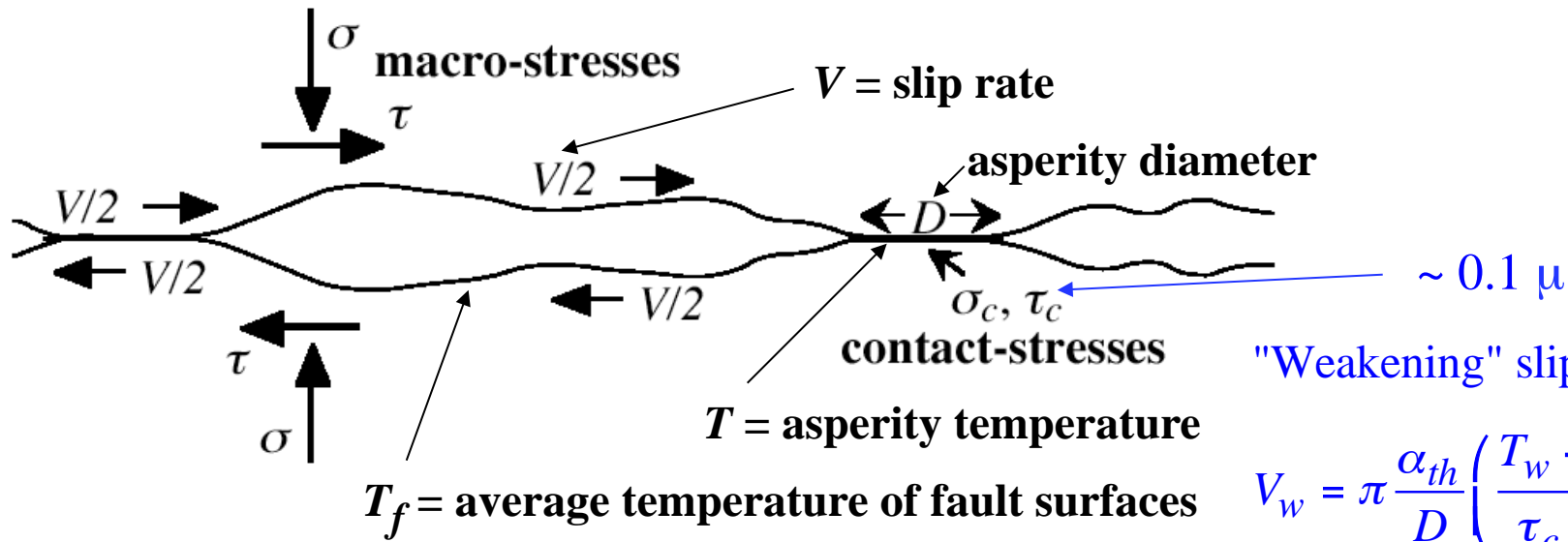
- *Another weakening process expected to be important from start of seismic slip:*

- Flash heating of asperity contacts, reduces  $f$  in rapid slip.

**Most studied so far for bare surfaces in contact;  
recent extensions to fault gouge**

# Flash heating of microscopic frictional asperity contacts

[Rice, AGU 1999; JGR 2006; Beeler and Tullis, AGU 2003, Beeler et al. JGR 2008, building on Bowden and Thomas, 1954; Archard, 1958/59; Ettles, 1986; Lim and Ashby, 1987.]



"Weakening" slip rate:

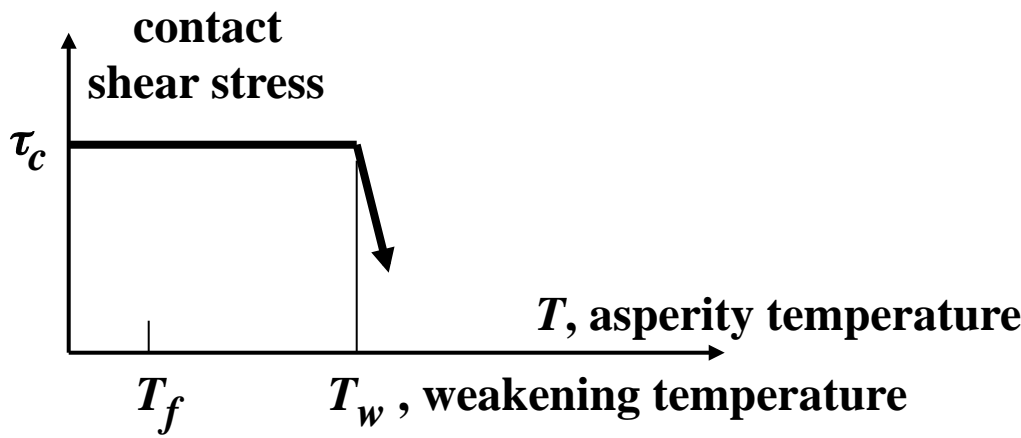
$$V_w = \pi \frac{\alpha_{th}}{D} \left( \frac{T_w - T_f}{\tau_c / \rho c} \right)^2$$

When  $V > V_w$ , asperity is weak for some of its life; suggests friction coef

$$f \approx f_{slow} \frac{V_w}{V} + f_{weak} \left( 1 - \frac{V_w}{V} \right)$$

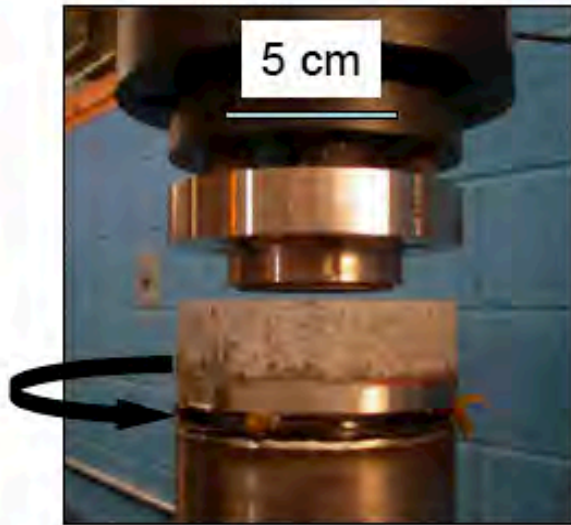
$$= f_{weak} + (f_{slow} - f_{weak}) \frac{V_w}{V}$$

when  $V > V_w$ .



[Tullis & Goldsby, *SCEC*, 2003; *EOS*, 2003]

## Rotary Shear Apparatus



High speed  $V \leq 0.36$  m/s

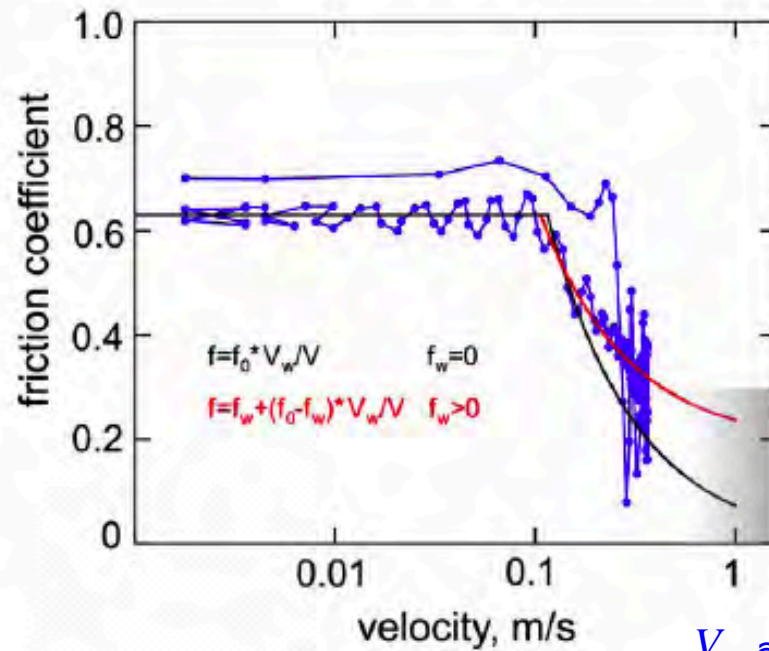
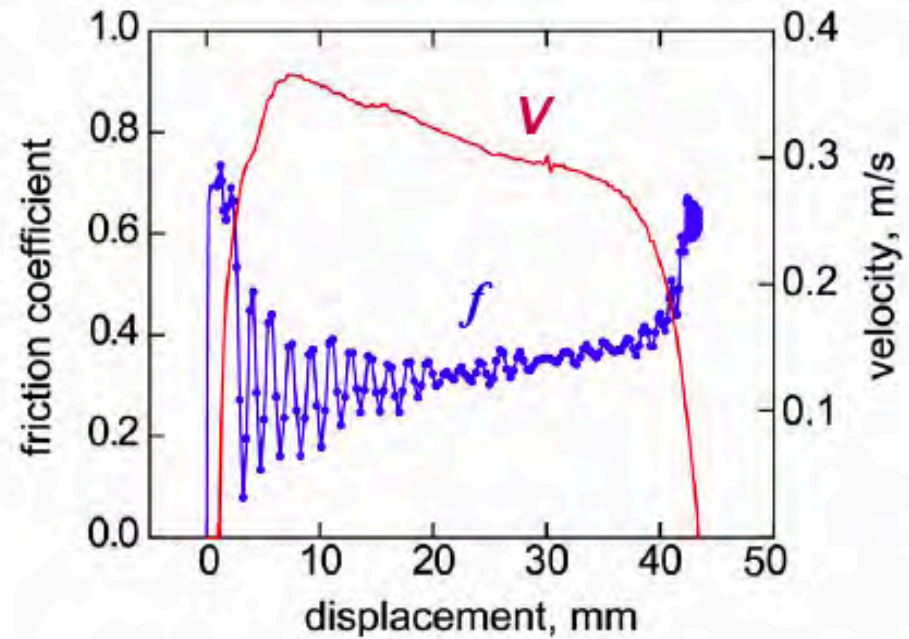
$\sigma_n = 5$  MPa

Rotary shear, 1.2 mm pre-slip at  $\sim 10$   $\mu\text{m/s}$ , followed by rapid slip for remaining 43 mm.

At low  $V$ ,  $f \approx 0.65$

At  $V > 0.3$  m/s,  $f \approx 0.30$

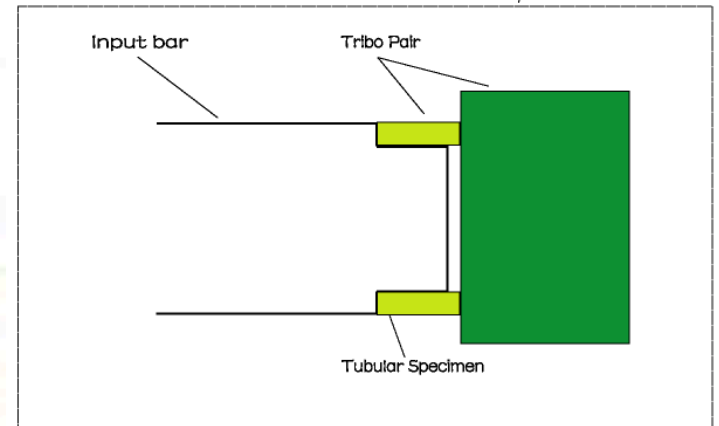
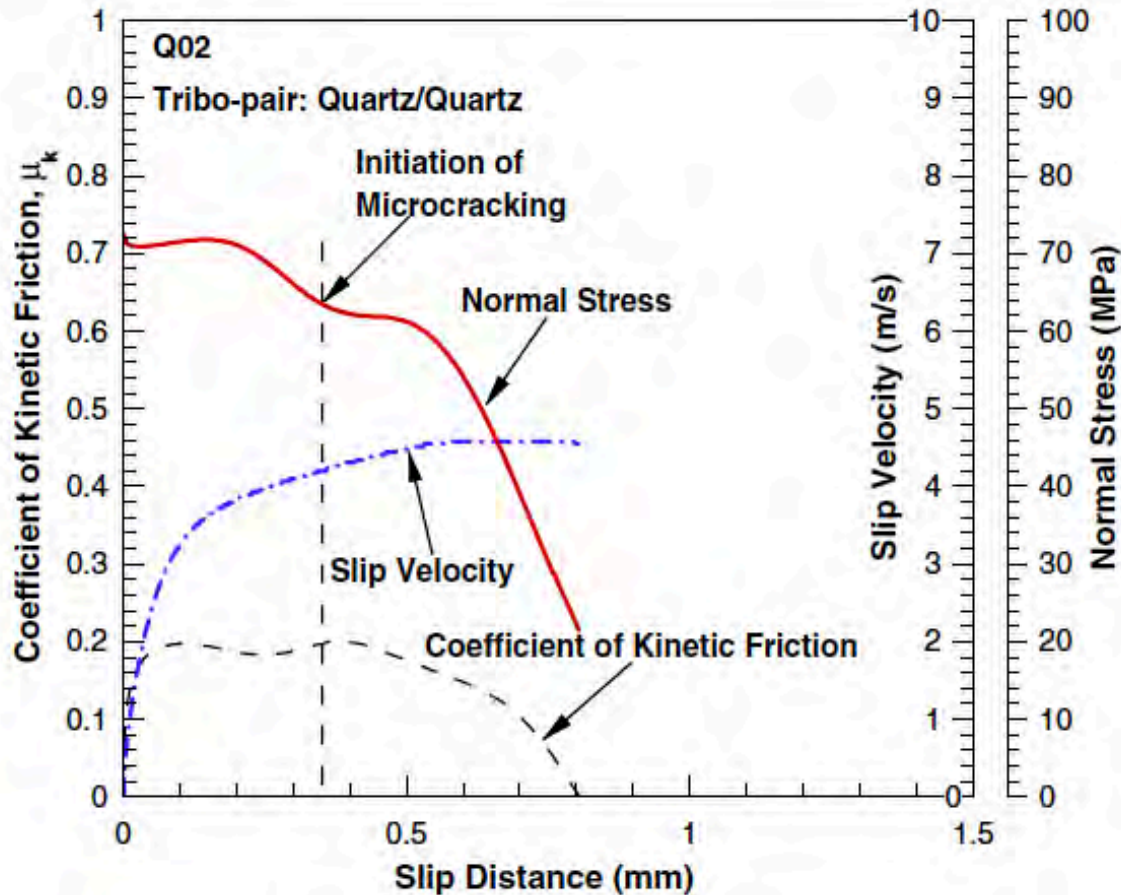
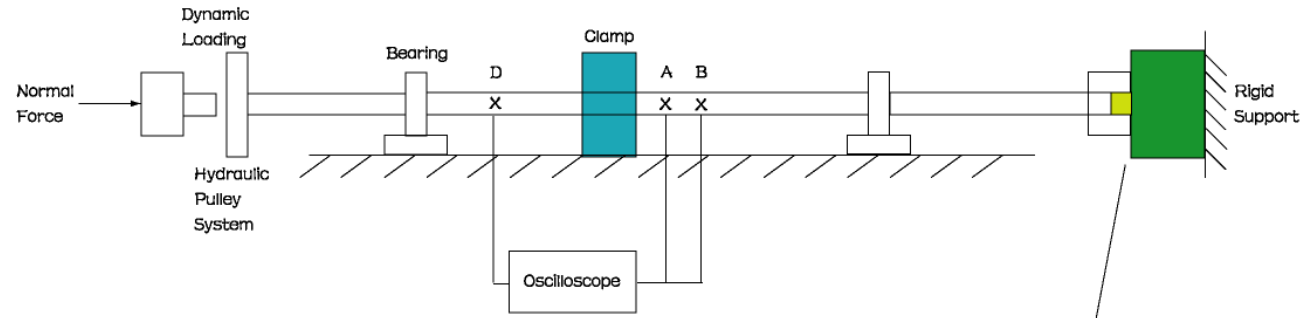
*Arkansas novaculite* ( $\sim 100\%$  quartzite)



$V_w \approx 0.14$  m/s

# Torsional Kolsky bar apparatus

[Yuan & Prakash, *Int. J. Solids & Structures*, 2008]



*Arkansas novaculite (quartzite)*

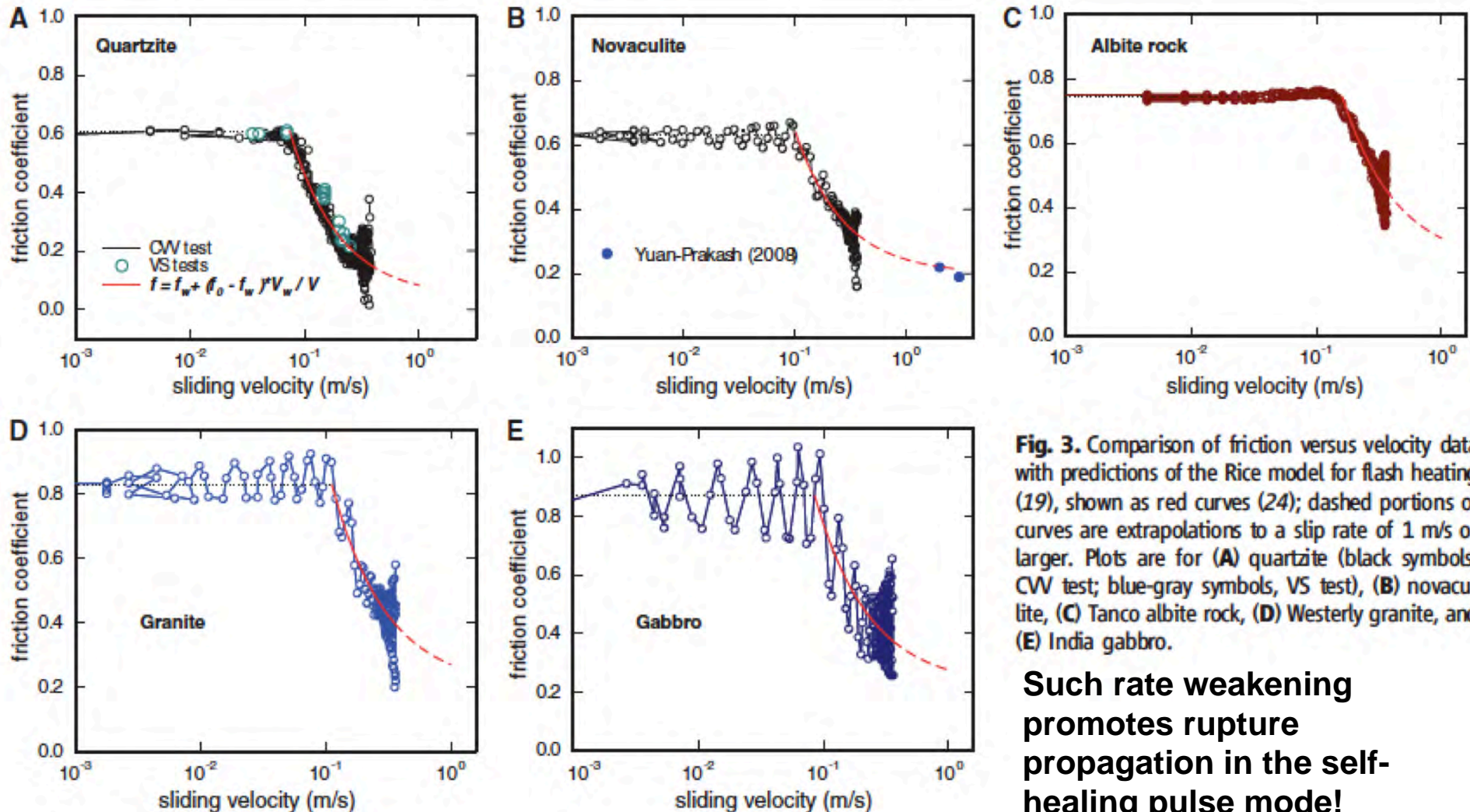
(Experiment becomes uninterpretable after small slip, marked, due to cracking in wall of specimen.)

Slip at  $V \approx 2-4$  m/s, resulting in  $f \approx 0.20$ .

# Goldsby & Tullis [Sci., 2011]:

## Test of simple flash weakening model,

$$f = f_o \text{ for } V < V_w, \quad f = f_w + (f_o - f_w) V_w / V \text{ for } V > V_w$$



**Fig. 3.** Comparison of friction versus velocity data with predictions of the Rice model for flash heating (19), shown as red curves (24); dashed portions of curves are extrapolations to a slip rate of 1 m/s or larger. Plots are for (A) quartzite (black symbols, CW test; blue-gray symbols, VS test), (B) novaculite, (C) Tanco albite rock, (D) Westerly granite, and (E) India gabbro.

**Such rate weakening promotes rupture propagation in the self-healing pulse mode!**



## Flash heating and weakening in gouge?

### Some relevant studies:

Beeler, N., T. E. Tullis, and D. L. Goldsby (JGR, 2008): **Constitutive relationships and physical basis of fault strength due to flash heating**

A. H. Kohli, D. L. Goldsby, G. Hirth, and T. E. Tullis (JGR, 2011): **Flash weakening of serpentinite at near-seismic slip rates**

B. P. Proctor, T. M. Mitchell, G. Hirth, D. L. Goldsby, F. Zorzi, J. D. Platt, and G. Di Toro (JGR, 2014): **Dynamic weakening of serpentinite gouges and bare surfaces at seismic slip rates**

J. D. Platt, B. P. Proctor, T. M. Mitchell, G. Hirth, D. L. Goldsby, G. Di Toro, N. M. Beeler, and T. E. Tullis (AGU Abstr., 2014): **The role of gouge and temperature on flash heating and its hysteresis**

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**Major points:**

**Building on *Beeler et al.* [2008], total slip rate assumed to be shared between multiple frictional contacts.**

**Solving for the contact temperatures, flash heating occurs when the strain rate exceeds a critical rate. For a deforming zone 100 microns wide,  $V_w$  is ~4 m/s (vs. ~0.1 m/s for bare surfaces) → flash heating much less efficient in gouge than for bare surfaces.**

**The lower contact slip rate → longer contact lifetimes → wider thermal boundary layer thickness  $W$  at contact**

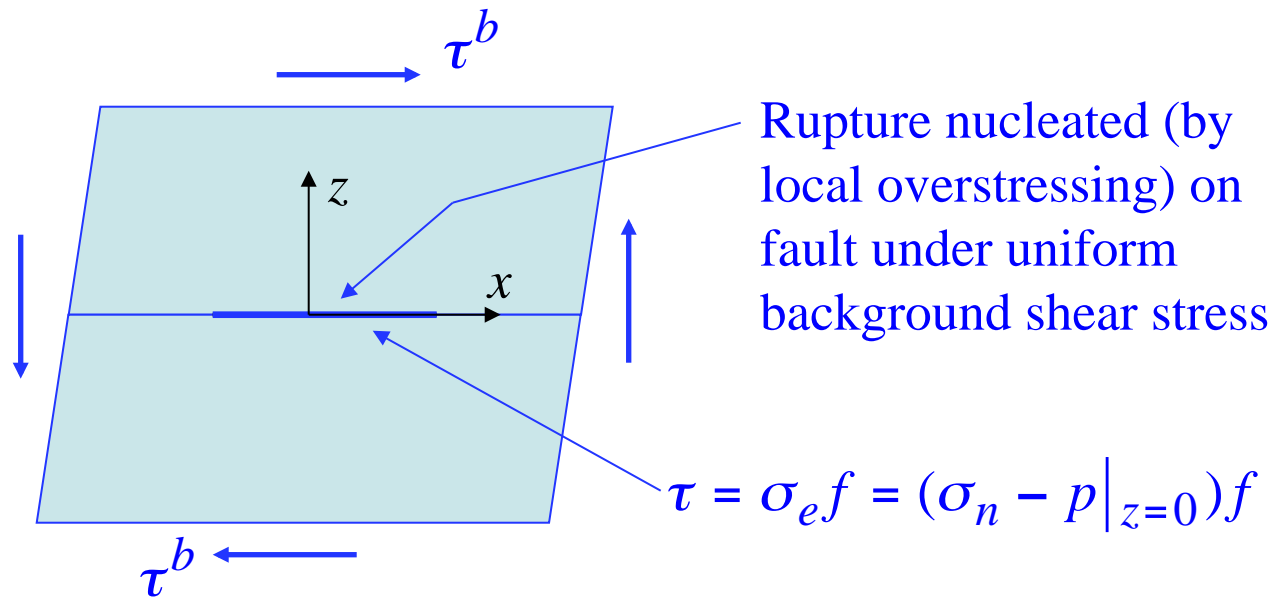
**When  $W \approx D$  (spacing between contacts) flash heating begins at much lower slip rates, and friction decreases slowly as the slip rate increases.**

**Hysteresis commonly seen in bare surface experiments, with higher friction observed during acceleration than deceleration. Accounting for the sensitive dependence of  $V_w$  on sliding surface temperature  $T_f$  allows to match some data for both acceleration and deceleration over a wide range of slip rates.**

# *Some Consequences for Earthquake Dynamics*

*Dynamic rupture simulations, incorporating flash heating of asperity contacts and thermal pressurization of pore fluid, with parameters constrained (to the extent possible) by laboratory observations*

[Noda, Dunham & Rice, *JGR* 2009]



# Flash heating (in dynamic rupture simulations, Noda, Dunham & Rice, JGR 09)

Effective stress law:

$$\tau = \sigma_e f = (\sigma_n - p|_{z=0}) f$$

*given, fixed compressive normal stress*

*friction coefficient*

*pore pressure on slip surface*

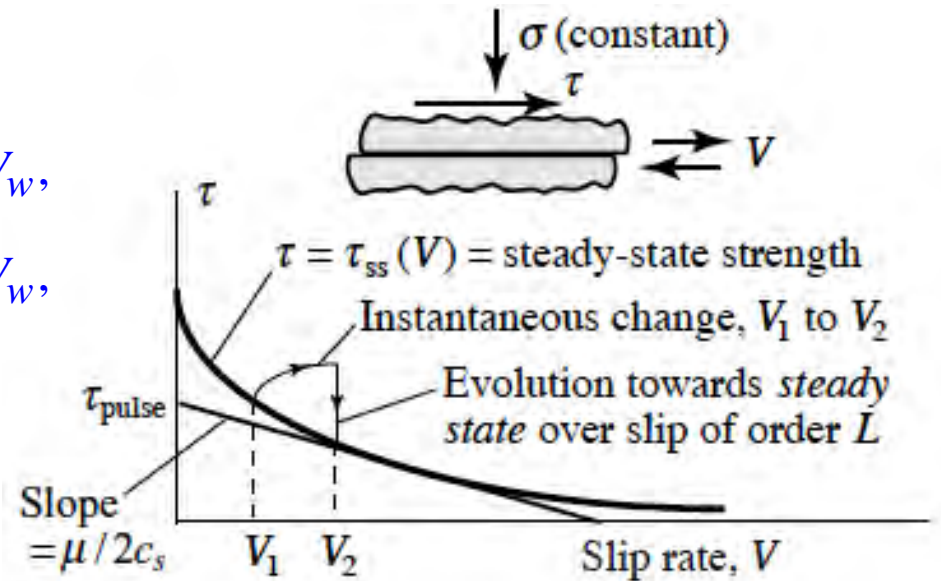
**Rate and state friction concepts, together with flash heating at microscopic contacts during rapid slip:**

$$\frac{df}{dt} = \frac{a}{V} \frac{dV}{dt} - \frac{V}{L} [f - f_{ss}(V)]$$

$$f_{ss}(V) = \begin{cases} f_{LV}(V), & V \leq V_w, \\ f_w + (f_{LV}(V) - f_w) \frac{V_w}{V}, & V \geq V_w, \end{cases}$$

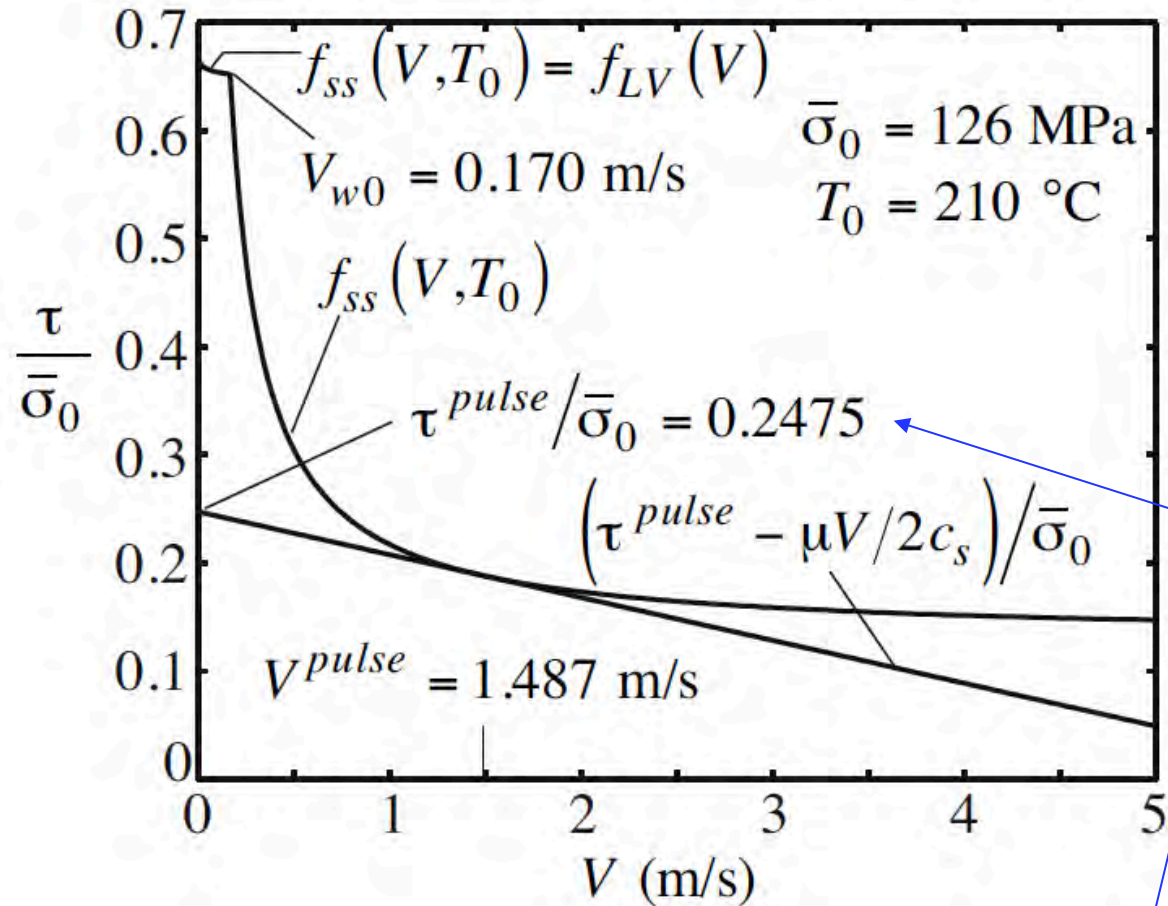
$$\text{with } V_w = \pi \frac{\alpha_{th}}{D} \left( \frac{T_w - T}{\tau_c / \rho c} \right)^2 ;$$

$$f_{LV}(V) = f_o + (a - b) \ln \left( \frac{V}{V_o} \right)$$



[Noda, Dunham & Rice, *JGR* '09]

**Based on Tullis and Goldsby [SCEC, '03] parameters  $f_o$ ,  $f_w$  and  $V_w$  for granite.**



**Figure 1.** Steady state frictional shear stress,  $\tau_{ss}$ , normalized by initial effective normal stress,  $\bar{\sigma}_0$ , as a function of slip velocity,  $V$ .  $\tau^{pulse}$  is defined for the initial ambient conditions at 7 km depth ( $T = 210$  °C,  $\sigma = 196$  MPa,  $p = 70$  MPa) by the radiation-damping line which fits tangentially to  $\tau_{ss}(V)$  at  $V = V^{pulse}$  ( $= 1.487$  m/s). The weakening slip rate is  $V_w = 0.170$  m/s. Due to extreme velocity weakening at elevated slip rates,  $\tau^{pulse}$  is very small ( $0.2475 \bar{\sigma}_0$ ).

Based on Zheng & Rice (BSSA, 1999), sustained rupture propagation expected to be possible, once nucleated, for background stress

$$\tau^b > \tau^{pulse} \approx 0.25 \bar{\sigma}_0$$

**Thermal pressurization** (in dynamic rupture simulations, Noda, Dunham & Rice, JGR 09)

**Effective stress law:**

$$\tau = \sigma_e f = (\sigma_n - p|_{z=0}) f$$

*given, fixed compressive normal stress*  
*friction coefficient*  
*pore pressure on slip surface*

**Thermal pressurization**, finite thickness of slipping zone, with Gaussian shear distribution having *r.m.s.* width  $w$ :

Conservation of energy  
(first law of thermodynamics):

$$\frac{\partial T}{\partial t} = \alpha_{th} \frac{\partial^2 T}{\partial z^2} + \frac{\tau}{\rho c} \frac{V}{\sqrt{2\pi} w} \exp\left(-\frac{z^2}{2w^2}\right)$$

Conservation of fluid mass  
(neglecting dilatancy):

$$\frac{\partial p}{\partial t} = \alpha_{hy} \frac{\partial^2 p}{\partial z^2} + \Lambda \frac{\partial T}{\partial t}$$

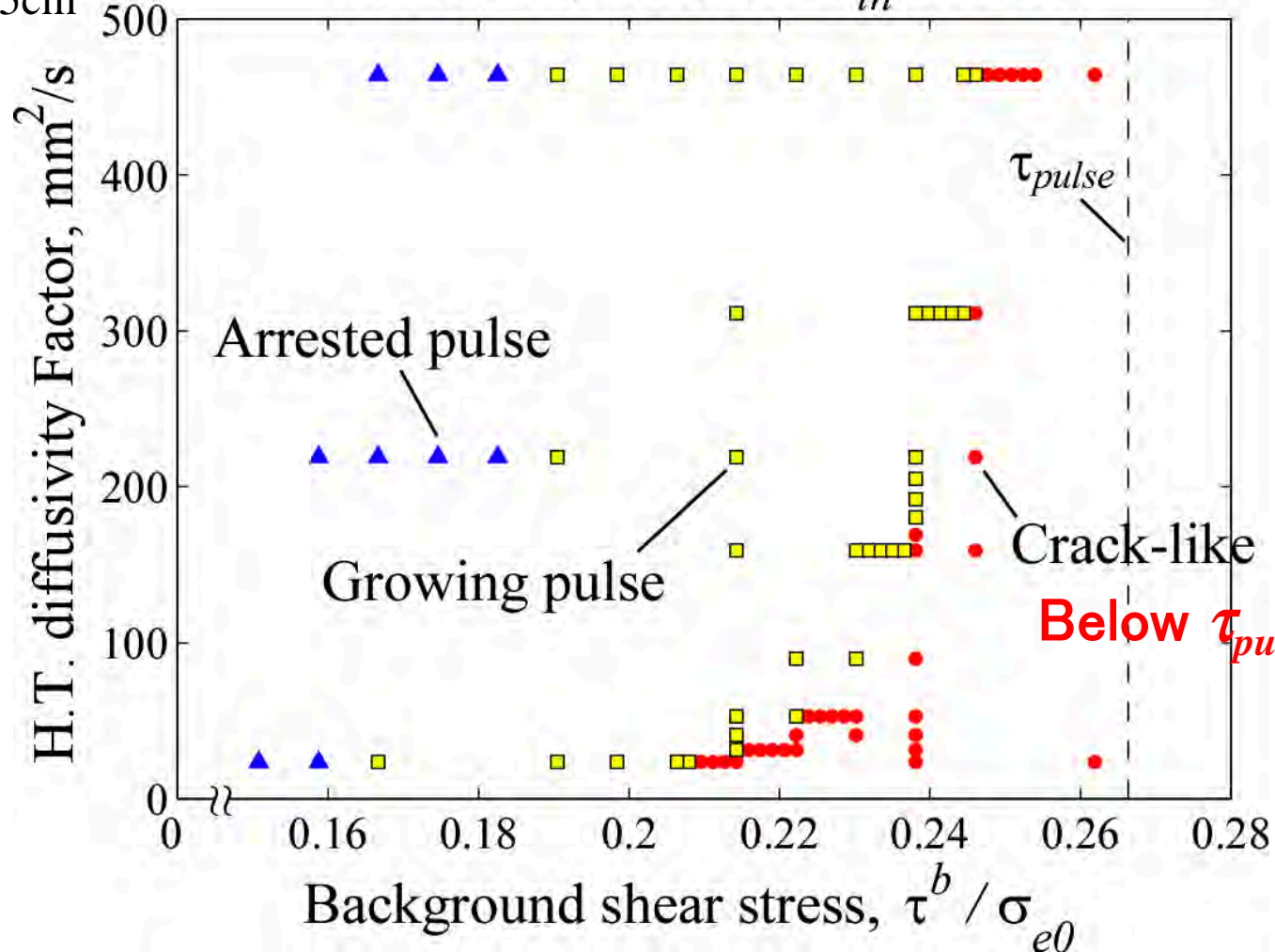
$\alpha_{th} \sim 0.7 \text{ mm}^2/\text{s}$ ;  $\alpha_{hy} \sim 0.9 - 6 \text{ mm}^2/\text{s}$  at mid-seismogenic depths;  $\rho c \sim 2.7 \text{ MJ}/\text{m}^3\text{K}$ ;  
 $\Lambda \sim 0.3 - 1.0 \text{ MJ}/\text{m}^3\text{K}$  (Rice [JGR 2006] & Rempel & Rice [*ibid*], based on Wibberley [EPS 2002, *priv comm* 2003] & Wibberley & Shimamoto [JSG 2003], and estimates of damage)

# Effect of hydrothermal properties

$\tau^{per} = 30\text{MPa}$

$D^{per} = 5\text{cm}$

Mode III, Different  $\alpha_{th}$  and  $\Lambda$



Shown:  
The case  
 $w = 0$ ,  
slip on a  
plane.

High  $\tau^b$  favors crack-like solution, thermal pressurization does too.

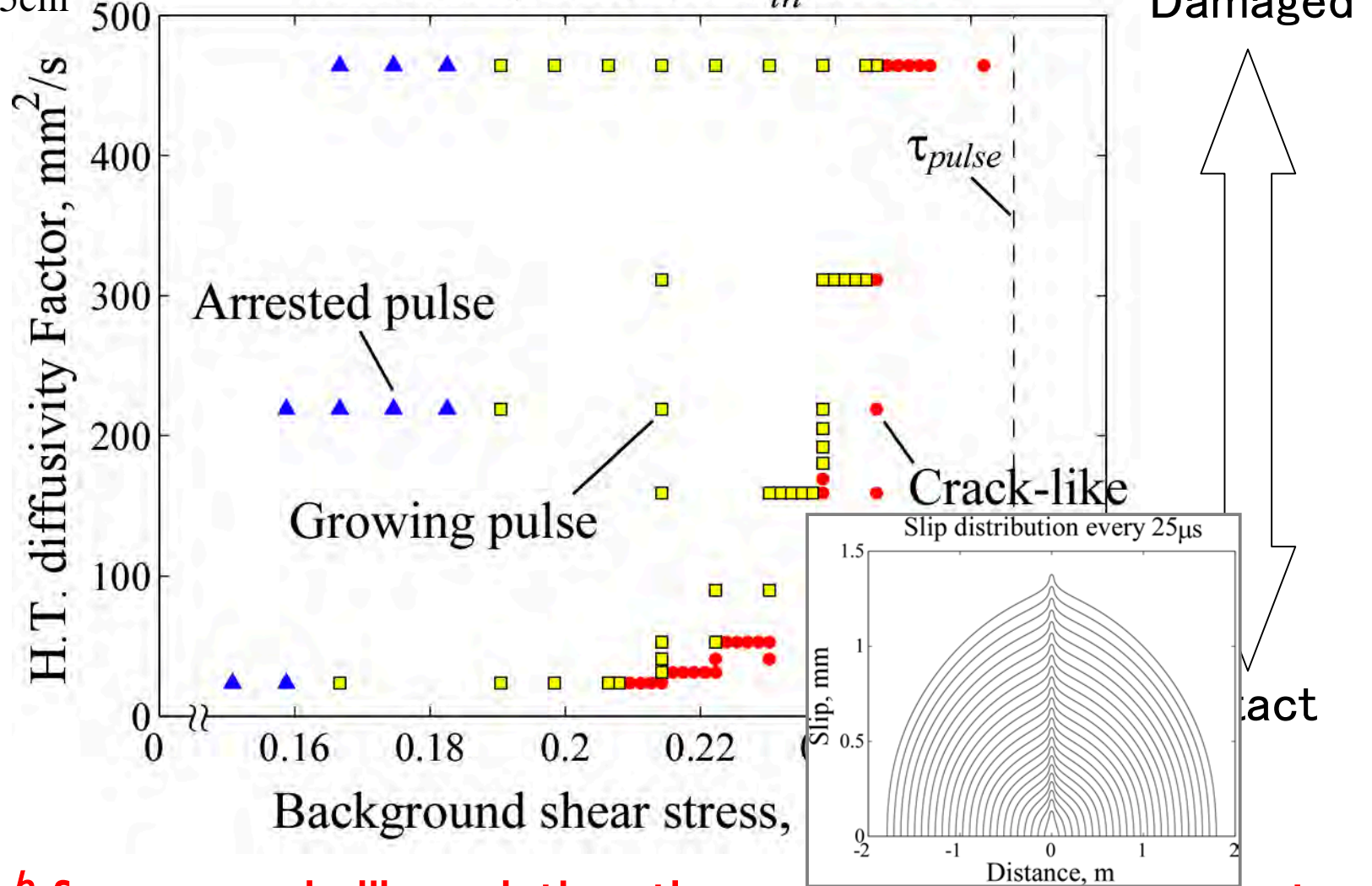


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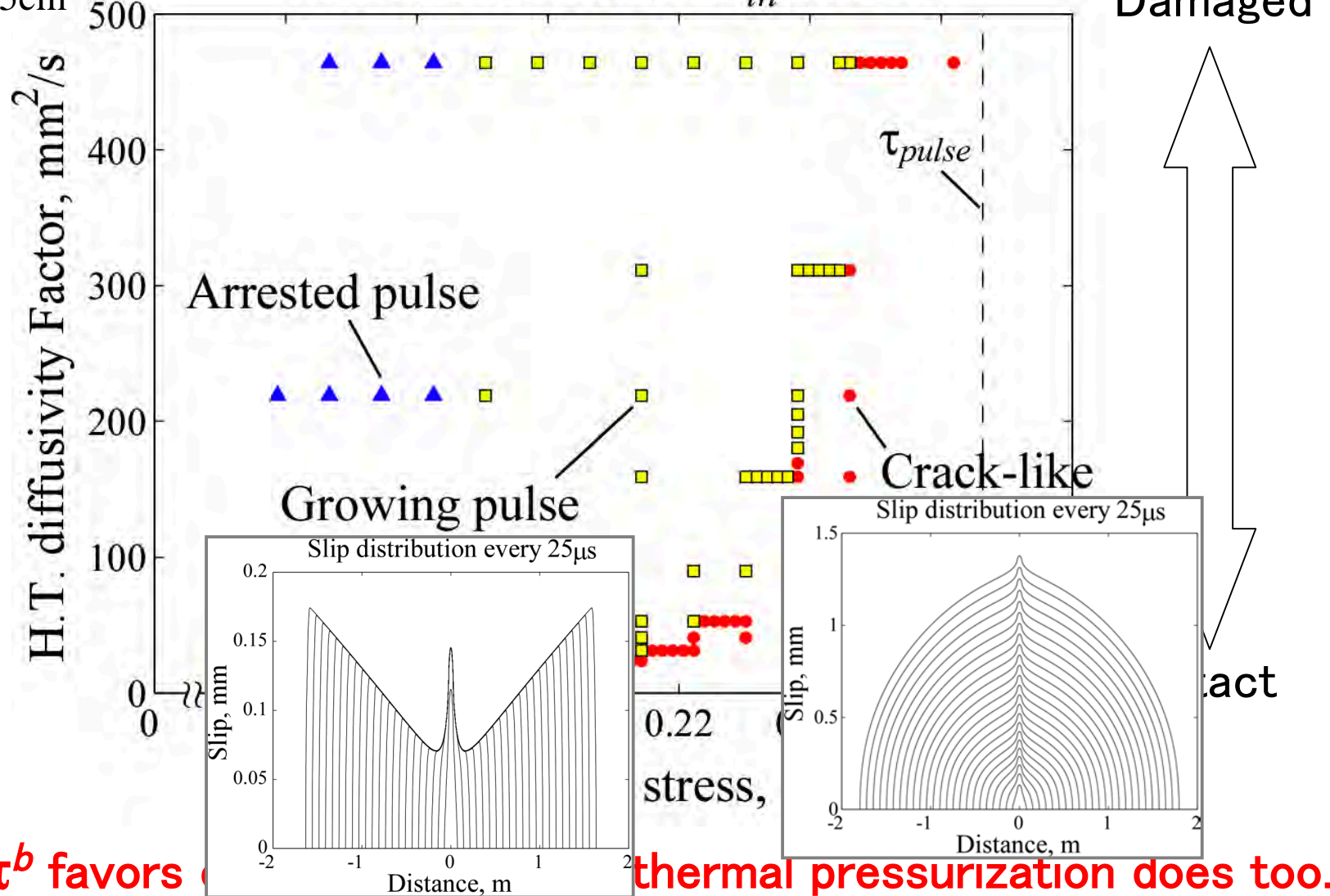
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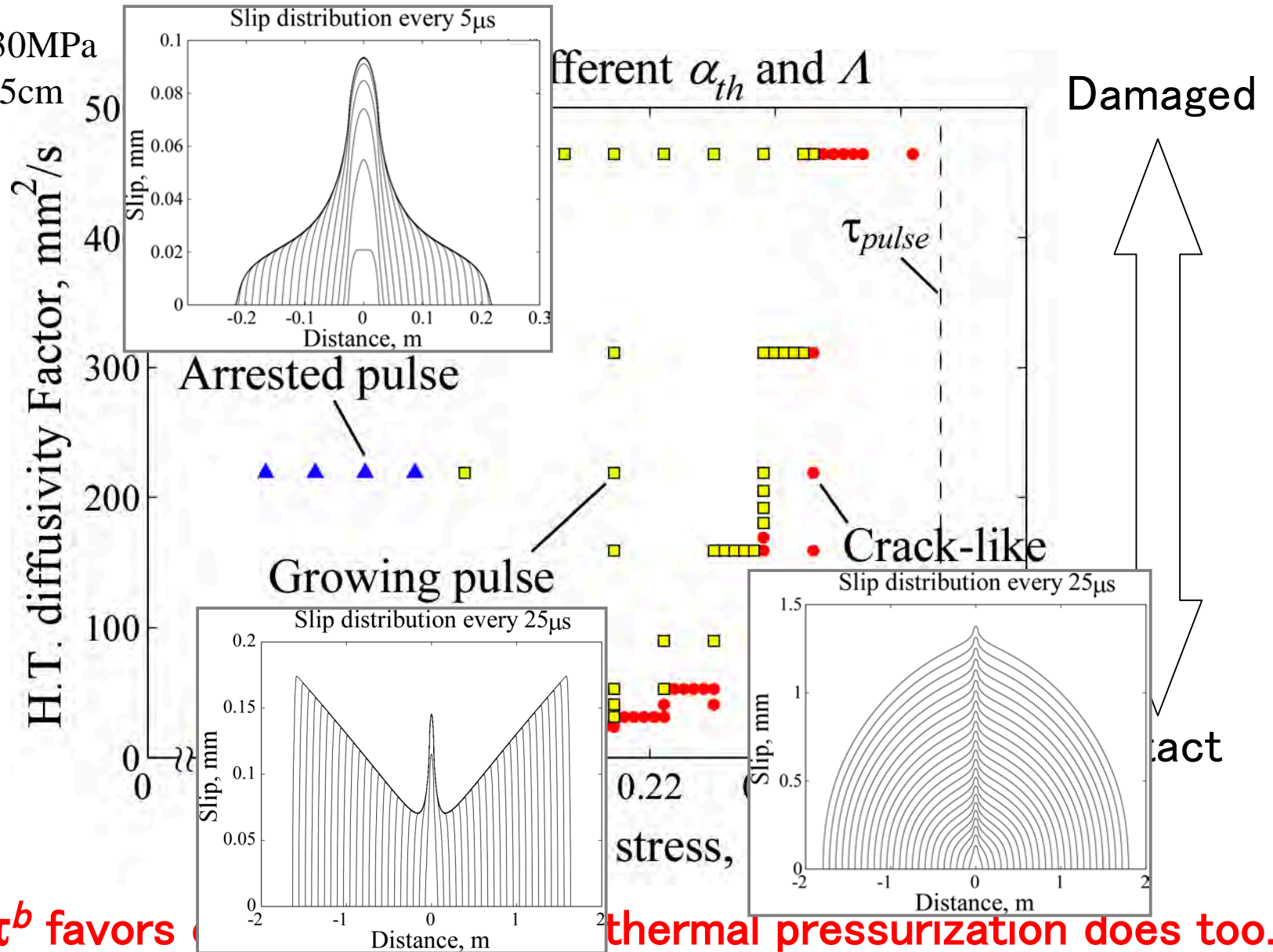


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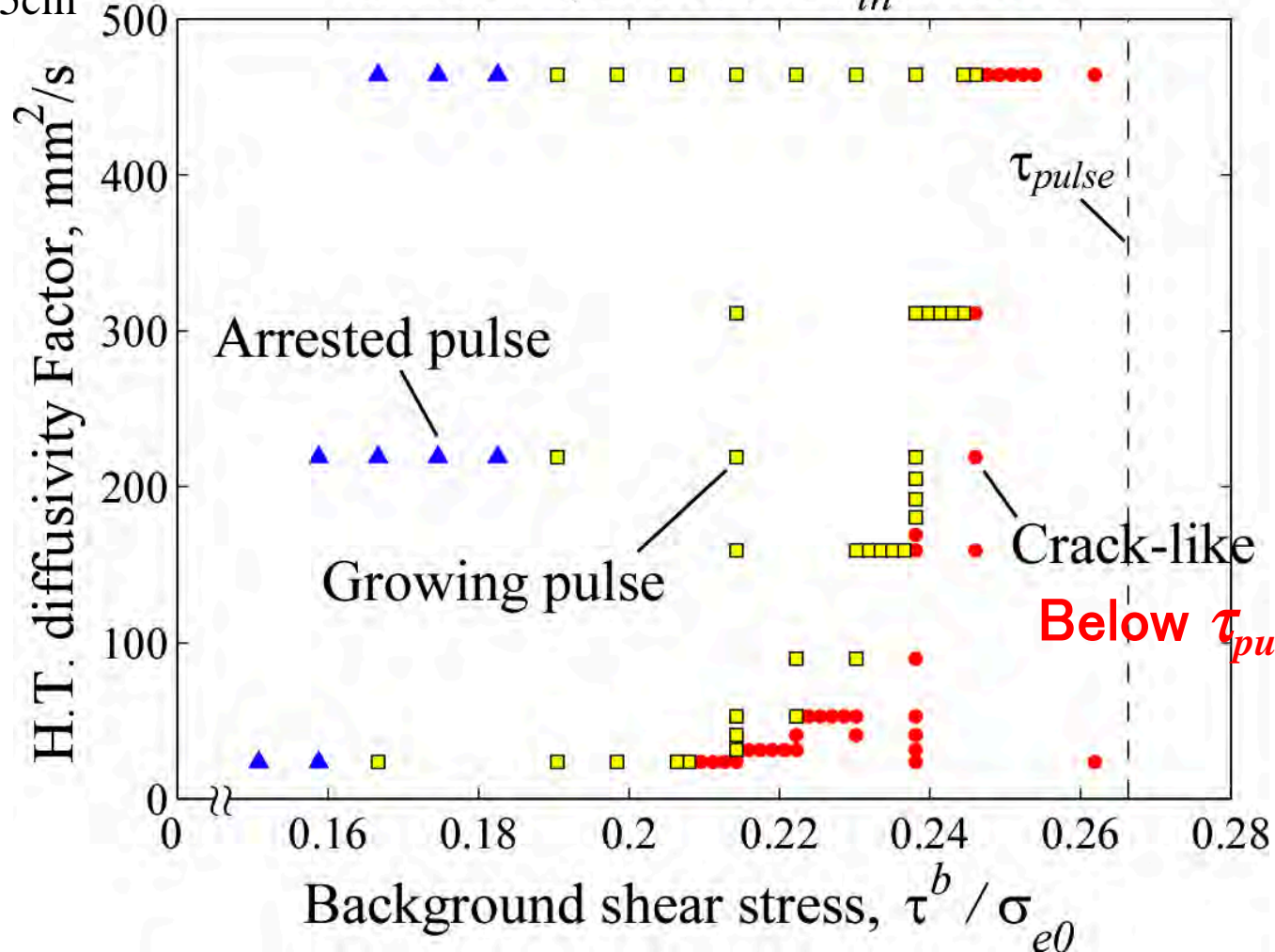
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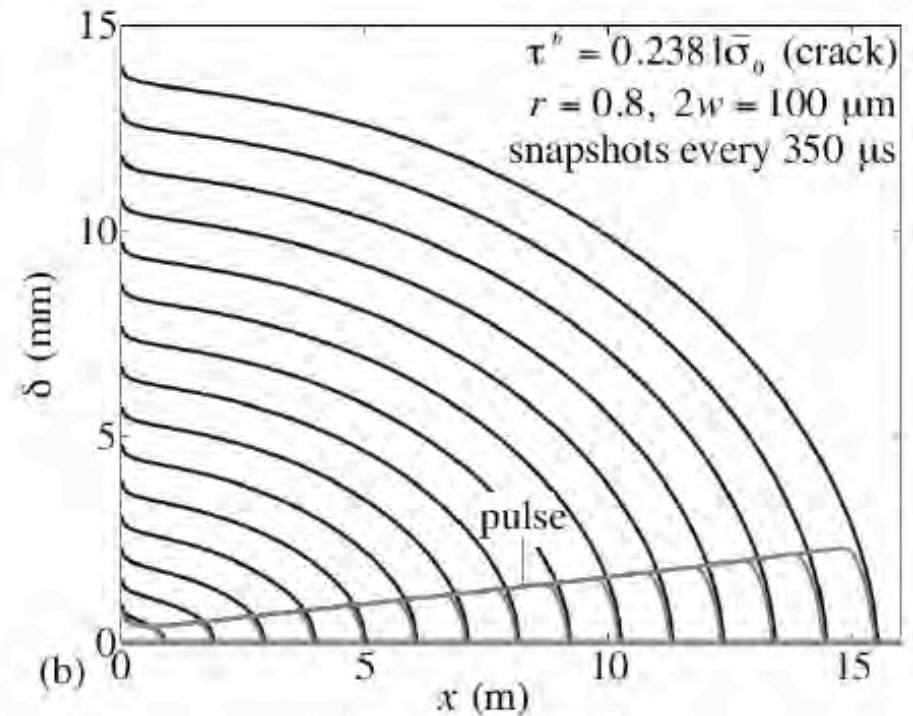
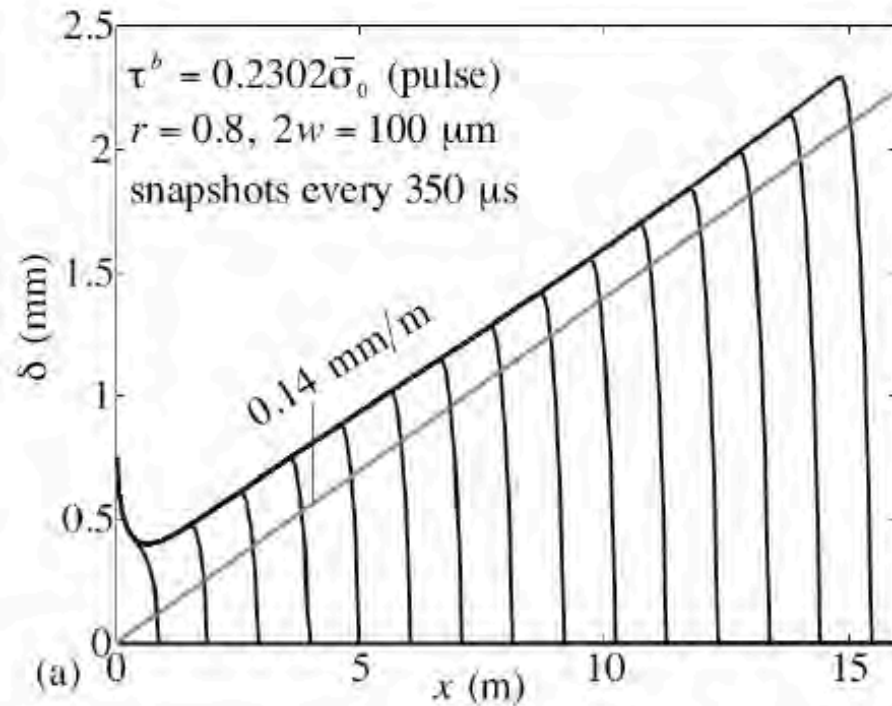


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High  $\tau^b$  favors crack-like solution, thermal pressurization does too.

Noda, Dunham & Rice [*JGR*, 2009]

Comparing a growing slip pulse at  $\tau^b = 0.230 (\sigma_0 - p_0)$   
to an enlarging shear crack at  $\tau^b = 0.238 (\sigma_0 - p_0)$



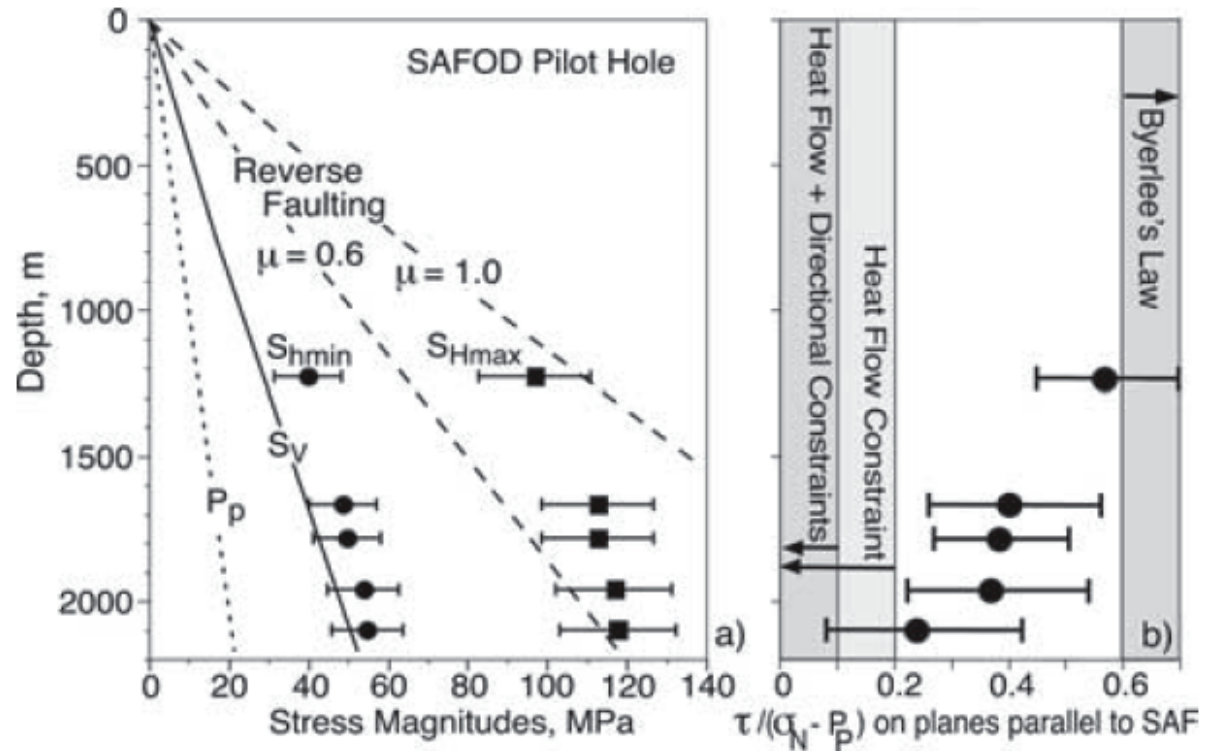
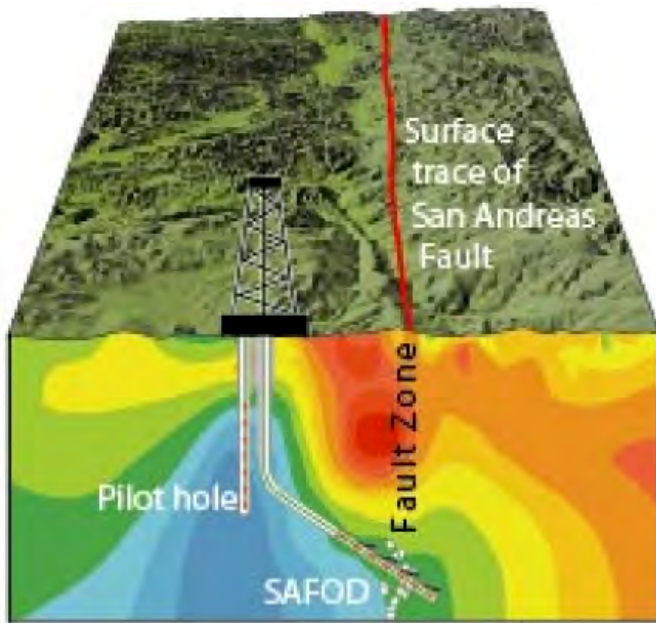
Both predict (if projected to circular fault) Seismic Moment  $M_o$  [Nm]  $\approx \lambda \times 10^{17} (t \text{ [s]})^3$ ;

$\lambda \approx 1.7$  for *slip pulse*,  $\lambda \approx 10.5$  for *crack*; compare,  $\lambda \approx 2$  for Parkfield 2004 [Uchide]

[Using  $\delta^{3D}/\delta^{2D} = 0.73$ ,  $\mu = 35$  GPa,  $\rho = 2800$  kg/m<sup>3</sup> ( $c_s = 3.5$  km/s), and  $v_r = 0.8c_s$ ]

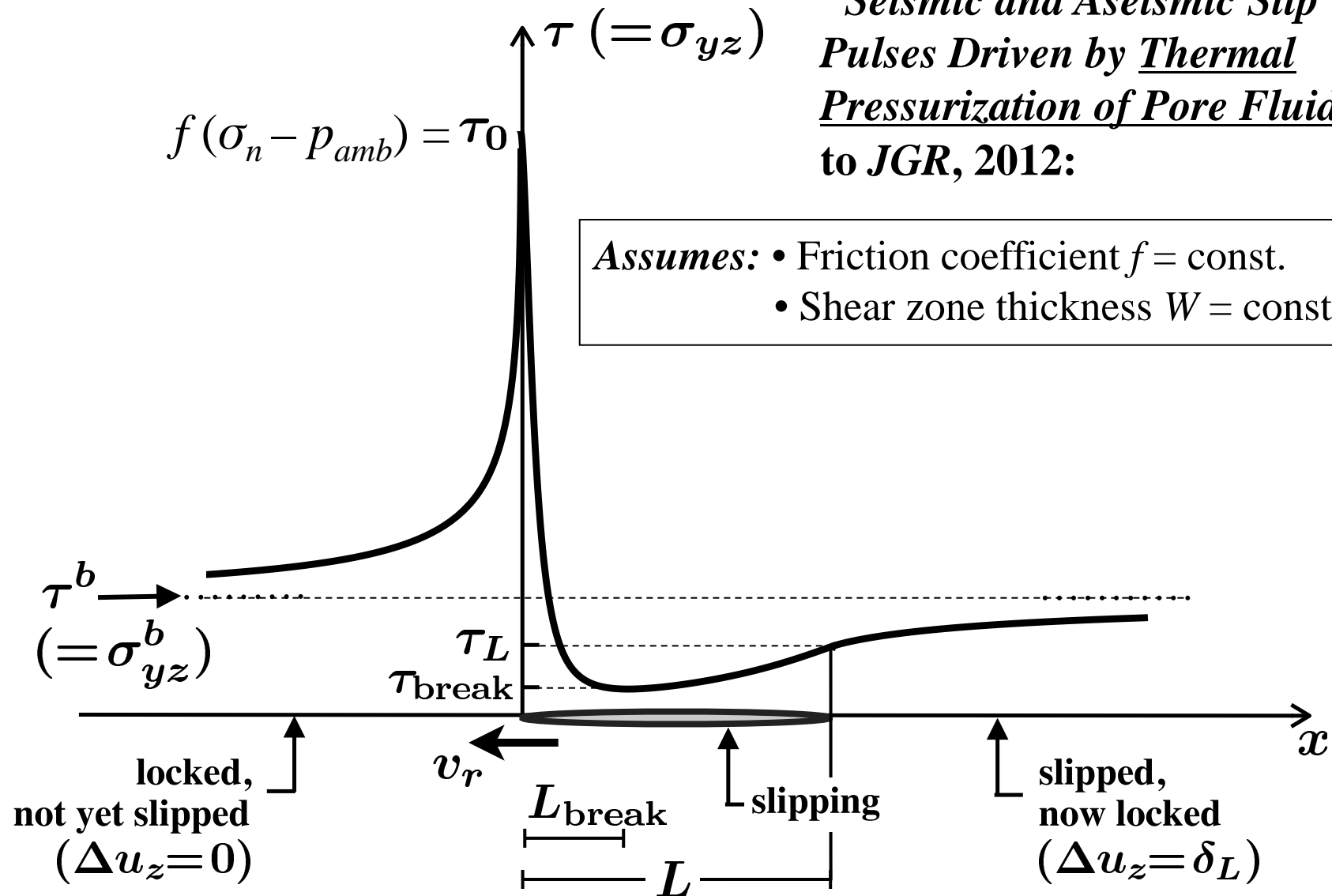
# Parkfield: San Andreas Fault Observatory at Depth

[Hickman & Zoback, *GRL* 2004]

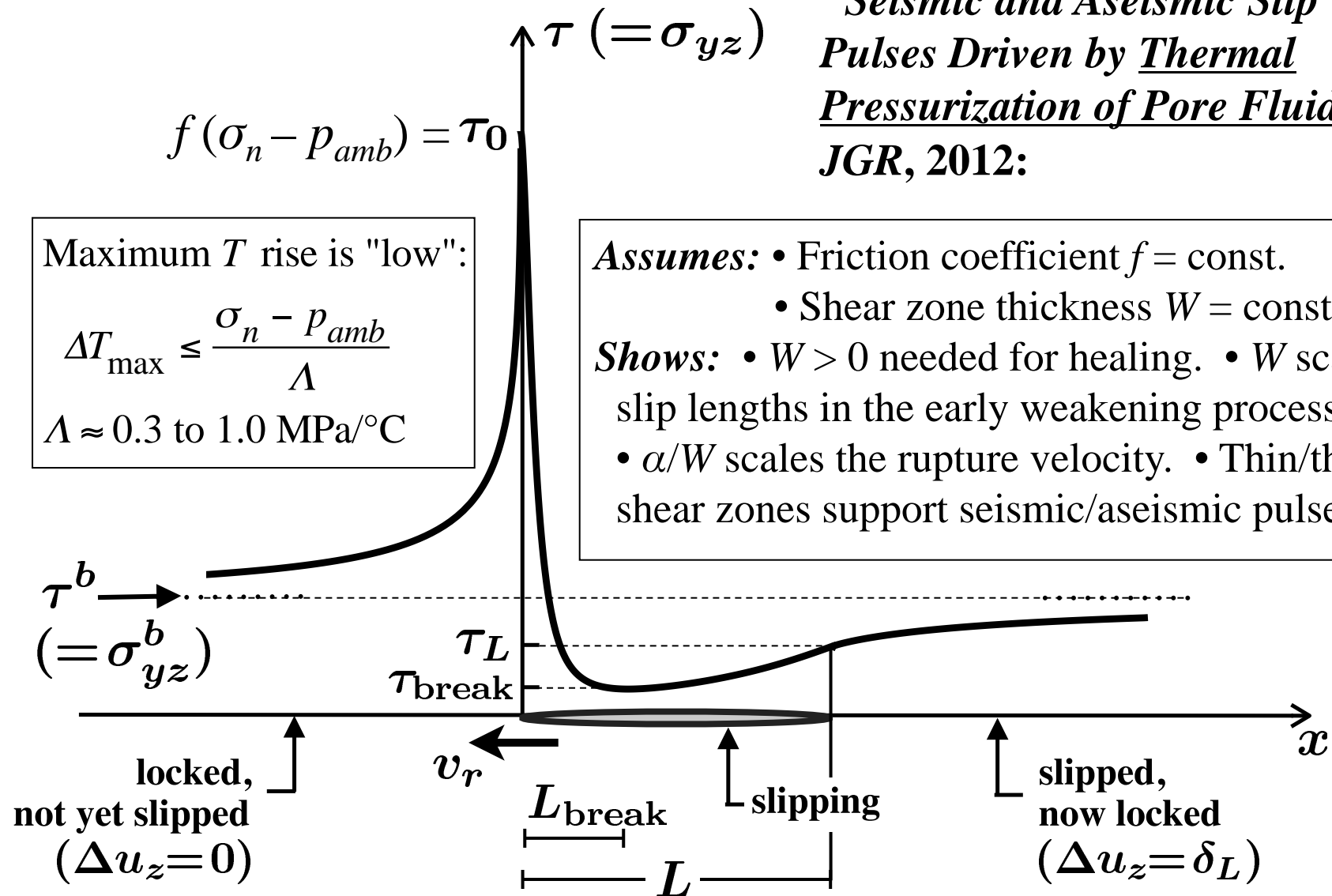


Simulations show growing pulse for  $\sim 0.22-0.24$

Steady-state pulse solutions,  
 from Dmitry I. Garagash,  
*"Seismic and Aseismic Slip  
 Pulses Driven by Thermal  
 Pressurization of Pore Fluid"*,  
 to *JGR*, 2012:



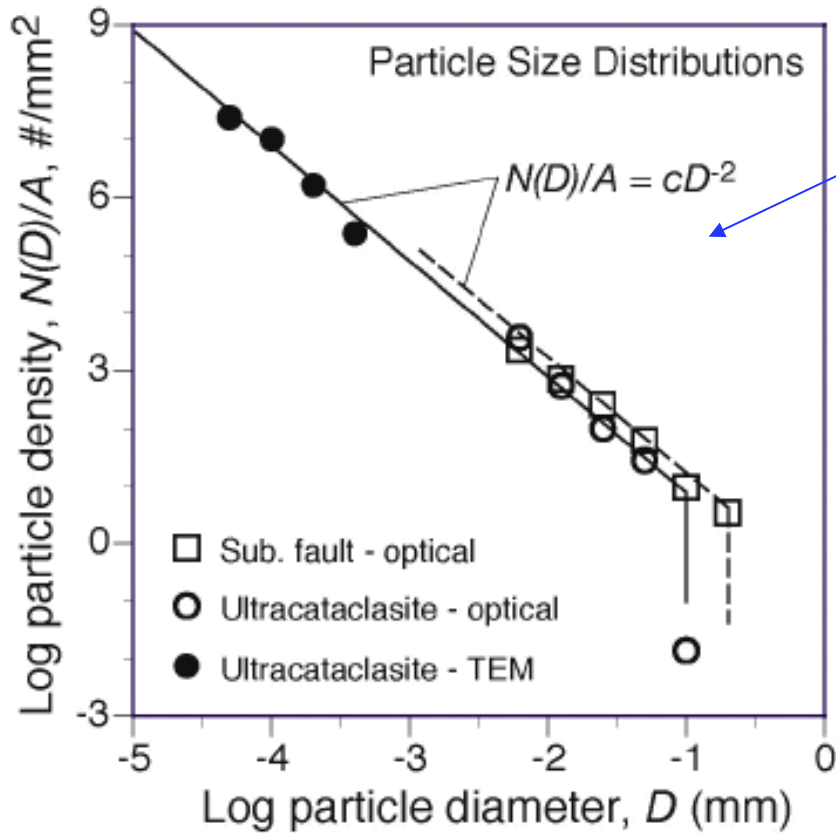
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## Conclusions:

- $\tau_{\text{static}}$  much larger than  $\tau_{\text{seismic}}$ .
- Documented weakening (and localization) processes:
  - flash heating;
  - thermal pressurization, in-situ & decomp product;
  - nanoparticle-related ←(physics remains unclear);
  - melting.
- Static strength  $\tau_{\text{static}} = f_s \sigma_n$  is unreliable predictor of pre-earthquake stress on major, well-slipped, smooth faults.
- Such faults may operate near or slightly above  $\tau_{\text{pulse}}$  (a  $\tau$  at which a small event, once nucleated, propagates indefinitely).
- Roughness may keep less mature faults from full benefit of dynamic weakening; to slip, side-walls must be deformed
- The fact that a segment is creeping does not preclude it from having large coseismic slip (Chi-Chi, 1999, Tohoku-Oki, 2011).



*Particle size distribution for Ultracataclasite gouge hosting the Punchbowl pss [Chester et al., Nature, 2005]*

- $N(D) / A =$  number of particles per unit sample area with  $2D / 3 < \text{diameter} < 4D / 3$ .

- $N(D) / A \approx c / D^2$  for  $30 \text{ nm} < D < 70 \mu\text{m}$ .

In 3D:  $\hat{N}(D) / V \approx \hat{c} / D^3$

- $D_{50}$  (= size such that 50% by mass are larger/smaller)  $\sim 1 \mu\text{m}$ .

- Standard granular material guideline (for narrow size range): thinnest possible shear zone  $\sim 5 \text{ to } 10 D_{50} \approx 5 \text{ to } 10 \mu\text{m}$

